

$B_{(c)} \rightarrow \tau\nu$: Complementarity at SuperB, LHC and LC

(+ issues in $B \rightarrow \pi K$)

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SuperBelle Meeting, KEK,
December 10th, 2008

$B_{(c)} \rightarrow \tau\nu$: Complementarity at SuperB, LHC and LC

(+ issues in $B \rightarrow \pi K$)

Stefan Recksiegel

from: TU München

speaking at: KEK

***R* Parity violating enhancement of
 $B_u^+ \rightarrow \ell^+ \nu$ and $B_c^+ \rightarrow \ell^+ \nu$**

Stefan Recksiegel
KEK Theory Group

LMU München

July 17th, 2002

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Recksiegel Stefan
あなたはKEKトリアスロン2002に於て頭書の成績を収めたのでこれを賞します
2002年9月21日
トリアスロン実行委員
川合将義
佐藤昌史



のでこれと賞します
平成 年 月 日
高エネルギー物理学研究所
所長 菅原寛彦

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- A. G. Akeroyd and S.R., J. Phys. G **29**, 2311 (2003)
 - A. G. Akeroyd, C. H. Chen and S.R., Phys. Rev. **D77**, 115018 (2008)
 - A. Buras, R. Fleischer, S.R. and F. Schwab, 2003-2006
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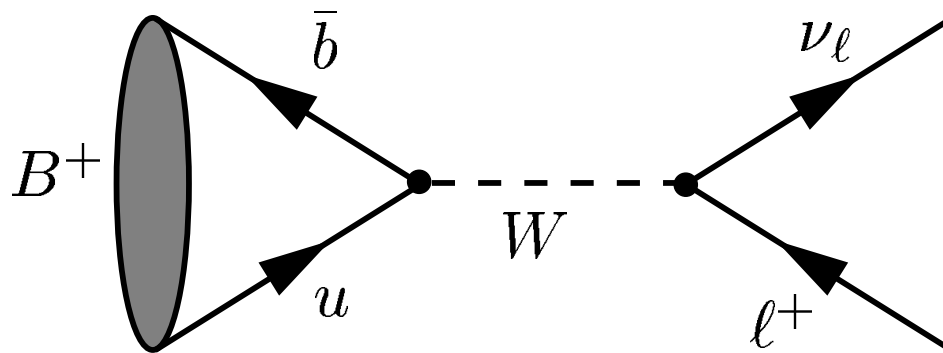
Why study $B \rightarrow \tau\nu$?

→ Suppressed in SM and clean (only f_B appears, no FFs).

Processes that are suppressed in the SM are excellent probes to look for New Physics, because they are not necessarily also suppressed in NP !

(This is why $b \rightarrow s\gamma$, B_0 - \bar{B}_0 mixing, $K \rightarrow \pi\nu\bar{\nu}$, etc. draw so much attention and why they are so good in constraining NP models.)

$$B_q^+ \rightarrow \ell^+ \nu_\ell$$



$B \rightarrow \tau \nu$ is suppressed so much because coupling to W is left-handed \rightarrow need spin-flip for the lepton \rightarrow factor m_ℓ

Standard Model rate for $B_q^+ \rightarrow \ell^+ \nu_\ell$:

$$\Gamma(B_q^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 m_{B_q} m_\ell^2 f_{B_q}^2 |V_{qb}|^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_{B_q}^2}\right)^2$$

Helicity suppression: BR is proportional to m_ℓ^2 , expect:

$$BR(B_q^+ \rightarrow \tau^+ \nu_\tau) : BR(B_q^+ \rightarrow \mu^+ \nu_\mu) : BR(B_q^+ \rightarrow e^+ \nu_e) = m_\tau^2 : m_\mu^2 : m_e^2$$

Experimentally,

$$\begin{aligned} BR(B^\pm \rightarrow \tau^\pm \nu_\tau) &= (1.70 \pm +0.42) \times 10^{-4} && \text{(BELLE-CONF-0840)} \\ &= (1.20 \pm 0.40 \pm 0.36) \times 10^{-4} && \text{(BaBar)} \end{aligned}$$

In agreement with the SM expectations, central values are

$$(\tau) 1.23 \times 10^{-4} : (\mu) 5.51 \times 10^{-7} : (e) 1.29 \times 10^{-11}$$

(Experimental limits on e, μ channels are 1, 1.3×10^{-6} , respectively.)

New Physics: 2HDM

The SM has only **one** Higgs doublet

→ masses for the gauge bosons and quarks, **one** physical particle.

Many other theories have **two Higgs doublets** (2HDM)

(SUSY needs two to provide masses to up- and down-quarks)

→ not **one** but **four** extra particles

h^0 has SM-like couplings m_f/v , H^0 , A^0 and H^\pm couplings are scaled by **$\tan \beta$** for down-type fermions (type-II 2HDM)

($\tan \beta$ is ratio of Higgs VEVs)

Let's look at this in a bit more detail:

Fermion Mass terms in the SM

$$\mathcal{L}_{\text{Yukawa}} = -\Gamma_u^{ij} \bar{Q}_L^i \phi^c u_R^j - \Gamma_d^{ij} \bar{Q}_L^i \phi d_R^j - \Gamma_e^{ij} \bar{L}_L^i \phi l_R^j + \text{h.c.}$$

(Γ_f are coupling matrices, Q_L^i and L_L^i are left-handed doublets, u_R^j, d_R^j, l_R^j are right-handed singlets)

The same scalar field gives the masses to **u-type** and **d-type** fermions

2HDM models:

$$\mathcal{L}_{\text{Yukawa}} = - \sum_{k=1,2} \Gamma_u^{ij,k} \bar{Q}_L^i \phi_k^c u_R^j - \sum_{k=1,2} \Gamma_d^{ij,k} \bar{Q}_L^i \phi_k d_R^j + \text{leptons} + \text{h.c.}$$

(ϕ_1 and ϕ_2 are the two Higgs fields)

Generally, **arbitrary couplings** to the two Higgs fields possible !

(“type-III 2HDM model”)

Problem: FCNC

Solution: Either u -type and d -type quarks both couple to same ϕ
→ “type-I 2HDM”

or u -type couple to ϕ_1 and d -type couple to ϕ_2 (e.g. SUSY)
→ “type-II 2HDM”

SUSY: Several more relations, among them: $M_h^2 \leq M_Z^2$ at tree level
→ obviously broken.

Loop corrections can relax bound to $M_h^{\max} \approx 135\text{GeV}$.

Important parameter: Ratio of VEVs of the two doublets

$$\tan \beta = v_1/v_2$$

Remember: In type-II, $\phi_1 \rightarrow u$ -type masses, $\phi_2 \rightarrow d$ -type masses

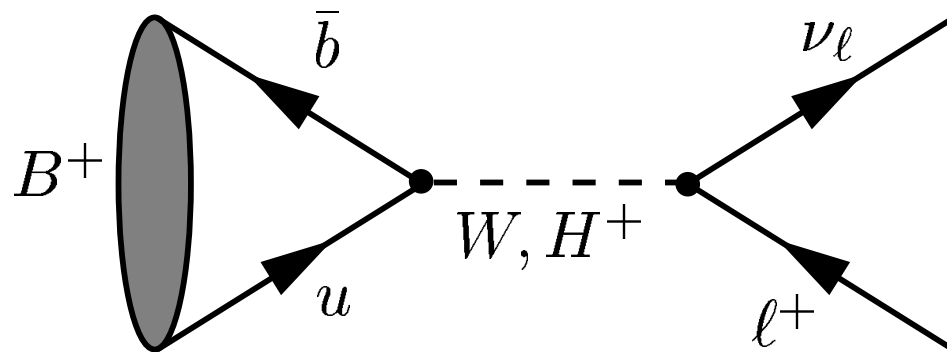
Large $\tan \beta \sim m_t/m_b$ allows top and bottom Yukawa coupling unification !

MSSM at large $\tan \beta$:

- Interesting effects on $B \rightarrow \tau \nu$
- Enhancement of $(g - 2)_\mu$ in accordance with exp
- No large non-SM effects in ΔM_{B_s} and $b \rightarrow s \gamma$
- $b \rightarrow s \ell^+ \ell^-$ can be strongly enhanced, but can be made compatible with experiment in parts of MSSM parameter space

$$B_q^+ \rightarrow \ell^+ \nu_\ell \text{ in 2HDMs}$$

Why are there interesting effects in $B^\pm \rightarrow \ell^+ \nu_\ell$?



H^\pm can mediate $B^\pm \rightarrow \ell^+ \nu_\ell$!

Factor m_ℓ also present, but now Yukawa, not helicity-flip.

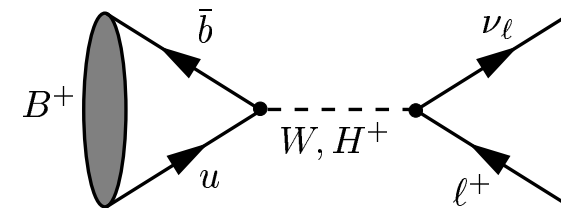
$\rightarrow \tan \beta$ enhancement

Effect of H^\pm on $B^\pm \rightarrow \ell^+ \nu_\ell$ modifies SM expression by factor r_H^q

$$r_H^q = \left[1 - \tan^2 \beta \frac{M_{B_q}^2}{M_{H^\pm}^2} \right]^2 \equiv [1 - R^2 M_{B_q}]^2$$

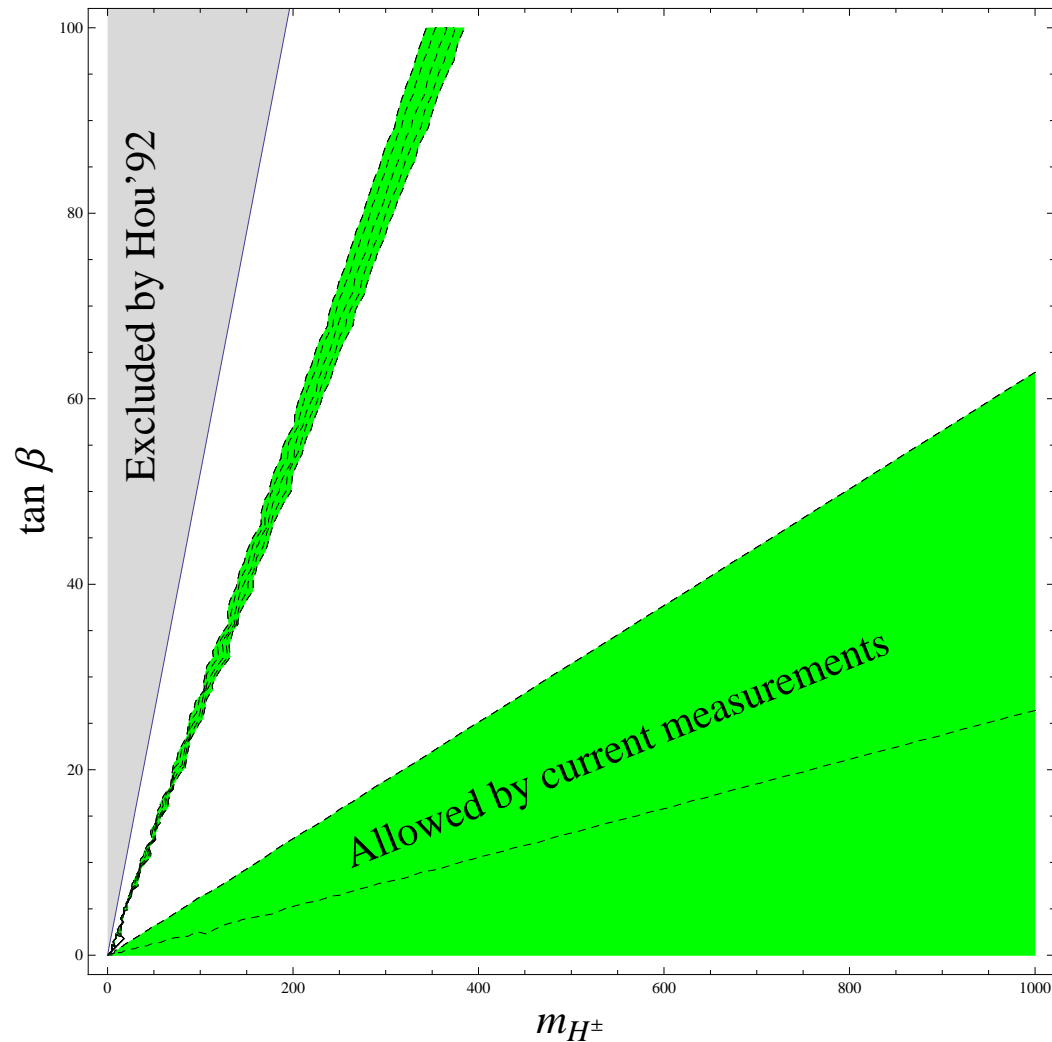
$\tan \beta \gg 1$ phenomenologically attractive,
significant contribution possible !

But: destructive interference, decreasing BR for small NP
contribution.



(Hou: $\tan \beta < 0.52 m_{H^-} / 1\text{GeV}$ for $BR(B \rightarrow \mu\nu) < 10^{-5}$ in 1992)

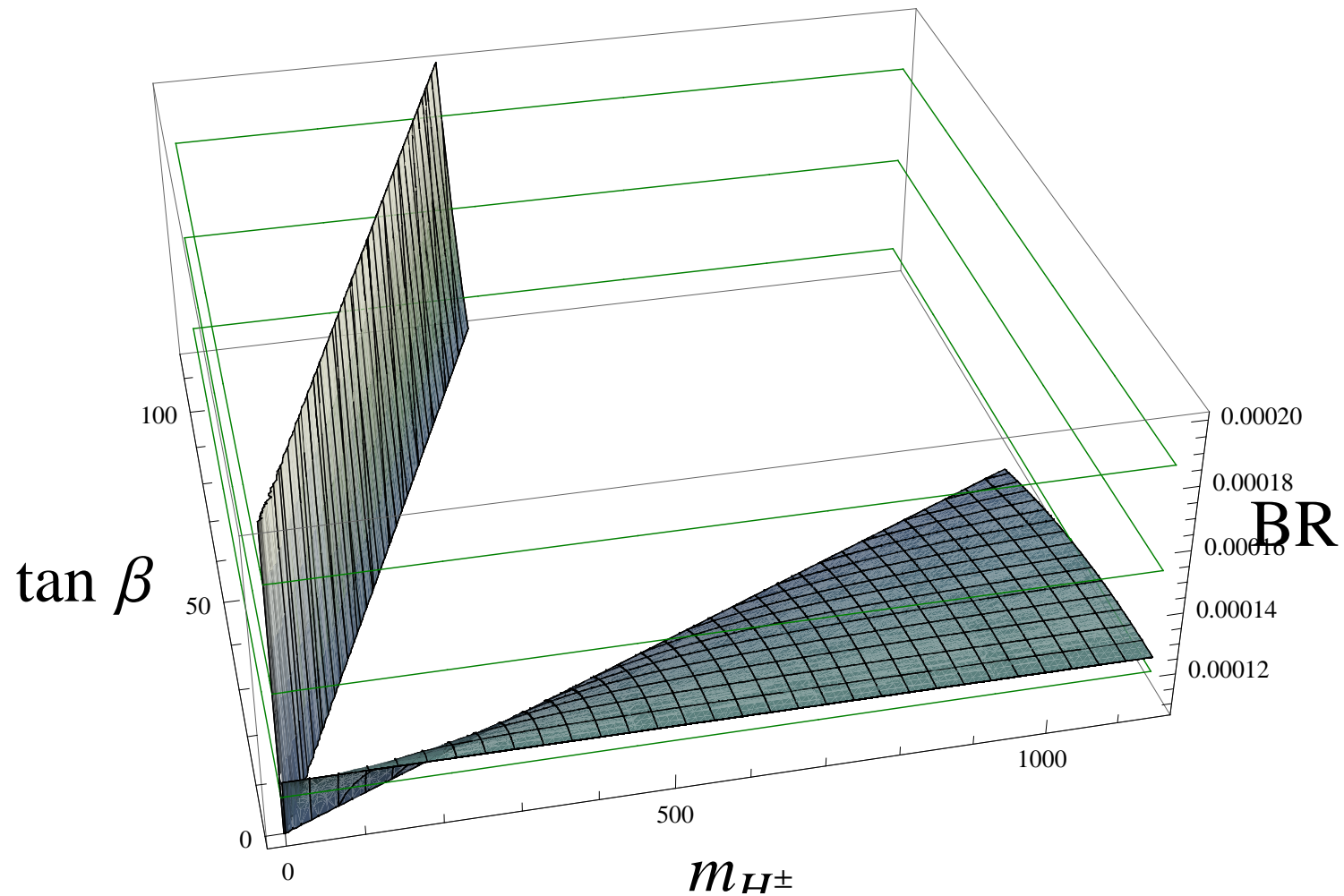
We plot the $M_{H^\pm} - \tan \beta$ plane:



Green: Allowed with 1- σ experimental range, f_B , BR_{exp} are varied in their 1- σ ranges (multiple lines)

(For clarity, we do not show areas excluded due to direct Higgs searches)

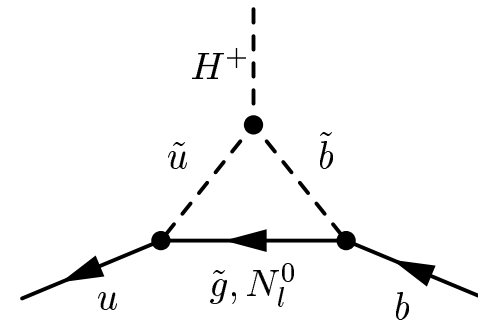
Why two allowed areas ? Let's look at this in 3D !



Green lines: 1- σ experimental range \rightarrow allowed area

Additional modification: vertex corrections, mainly gluino

$$r_H = \left(1 - \frac{\tan^2 \beta}{1 + \tilde{\epsilon}_0 \tan \beta} \frac{m_B^2}{m_{H^\pm}^2} \right)^2$$

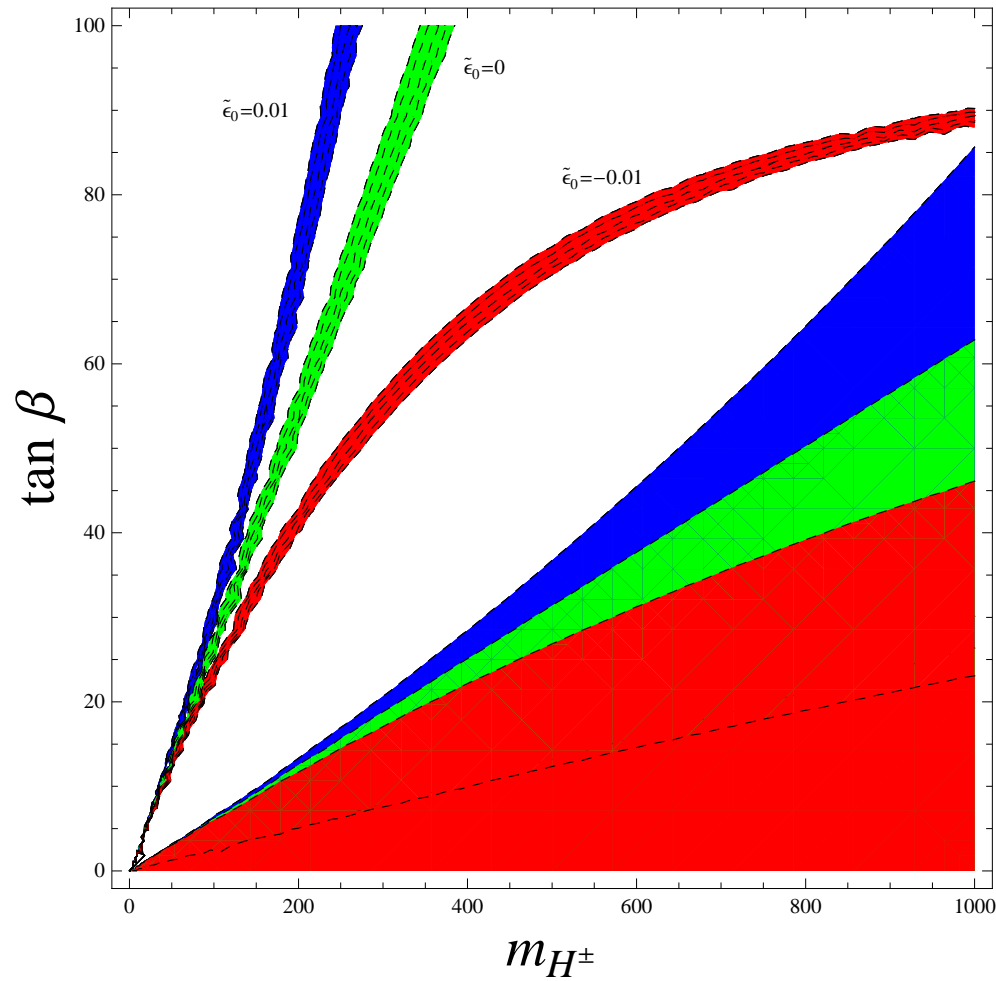


(A similar correction term can be generated at tree-level in type-III 2HDMs)

$\tilde{\epsilon}_0 \sim 10^{-2}$ is expected in MSSM

$\tilde{\epsilon}_0 < 0$ would be possible, but would involve $\mu < 0$ which moves $g - 2$ into the wrong direction

Still, let's look at what $\tilde{\epsilon}_0 = (0, \pm 10^{-2})$ does ...

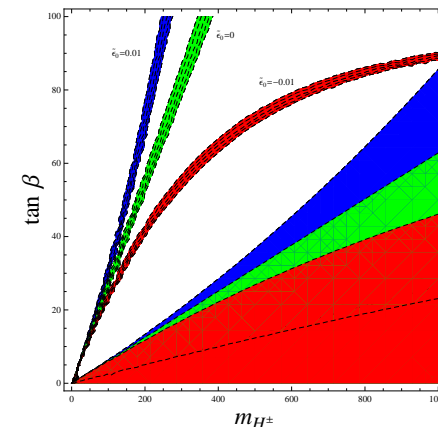


$$\tilde{\epsilon}_0 = (-10^{-2}, 0, 10^{-2})$$

$f_B, \text{BR}_{\text{exp}}$ are varied in their 1- σ ranges (multiple lines)
 \rightarrow very moderate dependence on $f_B, \text{BR}_{\text{exp}}$,
 but $\tilde{\epsilon}_0$ very important !

$B_u \rightarrow \tau\nu$ and 2HDMs

- We finally have a measurement of $B_u \rightarrow \tau\nu$
- In 2HDMs, H^+ contributions strongly modify $B \rightarrow \tau\nu$
 $\rightarrow B_u \rightarrow \tau\nu$ constrains parameter space of 2HDMs !
- Loop corrections (or even tree in type-III) can break the clean constraints in the $M_{H^\pm} - \tan\beta$ plane
- Careful when relating measurement \leftrightarrow constraints!



$$B_c \rightarrow \tau \nu$$

B_c not studied too well, cannot be produced in B factories

LEP had B_c in their samples \rightarrow how many ?

\Rightarrow do they influence the $\tan \beta / M_H$ -limits ?

Transition probability: $\approx 38\%$ of b -quarks hadronize into B_u^\pm ,

$2 \cdot 10^{-4} - 5 \cdot 10^{-3}$ hadronize into B_c^\pm

\rightarrow let us look a bit closer at that number

$$F_{b \rightarrow B_c}$$

Lisignoli/Masetti/Petrarca 1991

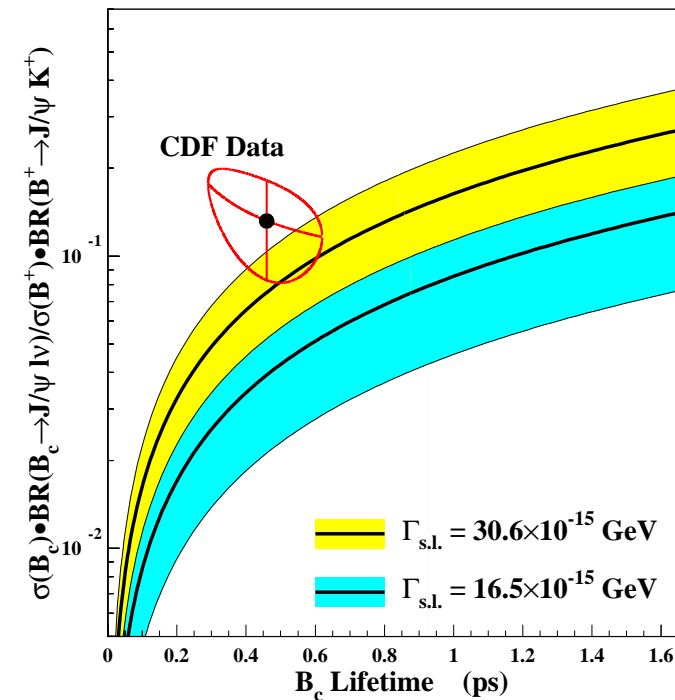
HERWIG Monte Carlo study:

$$F_{b \rightarrow B_c} \sim \begin{array}{ll} 0.2 - 1.0 \cdot 10^{-3} & @\text{LEP} \\ 1.3 \cdot 10^{-3} & @\text{Tevatron} \end{array}$$

CDF 1998

CDF: “Observation of B_c in $p\bar{p}$ ”: $F_{b \rightarrow B_c} = 1.3 \cdot 10^{-3}$

Data still significantly on the high side of theoretical predictions

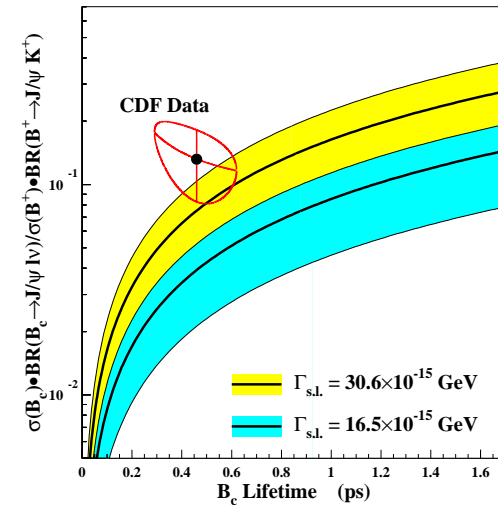


CDF 1998:

$$\frac{\sigma(B_c^+) \cdot \text{BR}(B_c \rightarrow J/\psi e^\pm \nu)}{\sigma(B^+) \cdot \text{BR}(B \rightarrow J/\psi K^+)} = 0.13 \pm 0.05$$

CDF/D0 2006:

$$\frac{\sigma(B_c^+) \cdot \text{BR}(B_c \rightarrow J/\psi e^\pm \nu)}{\sigma(B^+) \cdot \text{BR}(B \rightarrow J/\psi K^+)} = 0.28 \pm 0.07$$



Gershtein/Likhoded 07

Using CDF/D0 branching fractions for $B \rightarrow J/\psi K^\pm$ and $B_c \rightarrow J/\psi e^\pm \nu$, G/L claim that B_c production is “an order of magnitude higher” than theoretical predictions

$$F_{b \rightarrow B_c} = 1 \cdot 10^{-3} - 5 \cdot 10^{-3}$$

Analyses of $B \rightarrow \tau\nu$ before B_u channel measurement

L3 97

L3 gave a limit on $B_u \rightarrow \tau\nu$: (actually: $B_u \rightarrow \tau\nu + B_c \rightarrow \tau\nu$)
 $\text{BR}(B_u \rightarrow \tau\nu) < 5.7 \cdot 10^{-4}$ @ 90 % CL (i.e. ≈ 3.5 SM).

With this result, they improved Hou's '93 limit
($\tan\beta \leq 0.52 m_{H^-}/1\text{GeV}$) to $\tan\beta \leq 0.38 m_{H^-}/1\text{GeV}$

Mangano/Slabopitsky 97

took into account B_c contribution in L3 analysis !

Assumed $2 \cdot 10^{-4} - 1 \cdot 10^{-3}$ for $F_{b \rightarrow B_c}$, studied limits on $\tan\beta/M_H$.

$$\rightarrow \tan\beta \leq 0.3x m_{H^-}/1\text{GeV}, \quad 0 \leq x \leq 7$$

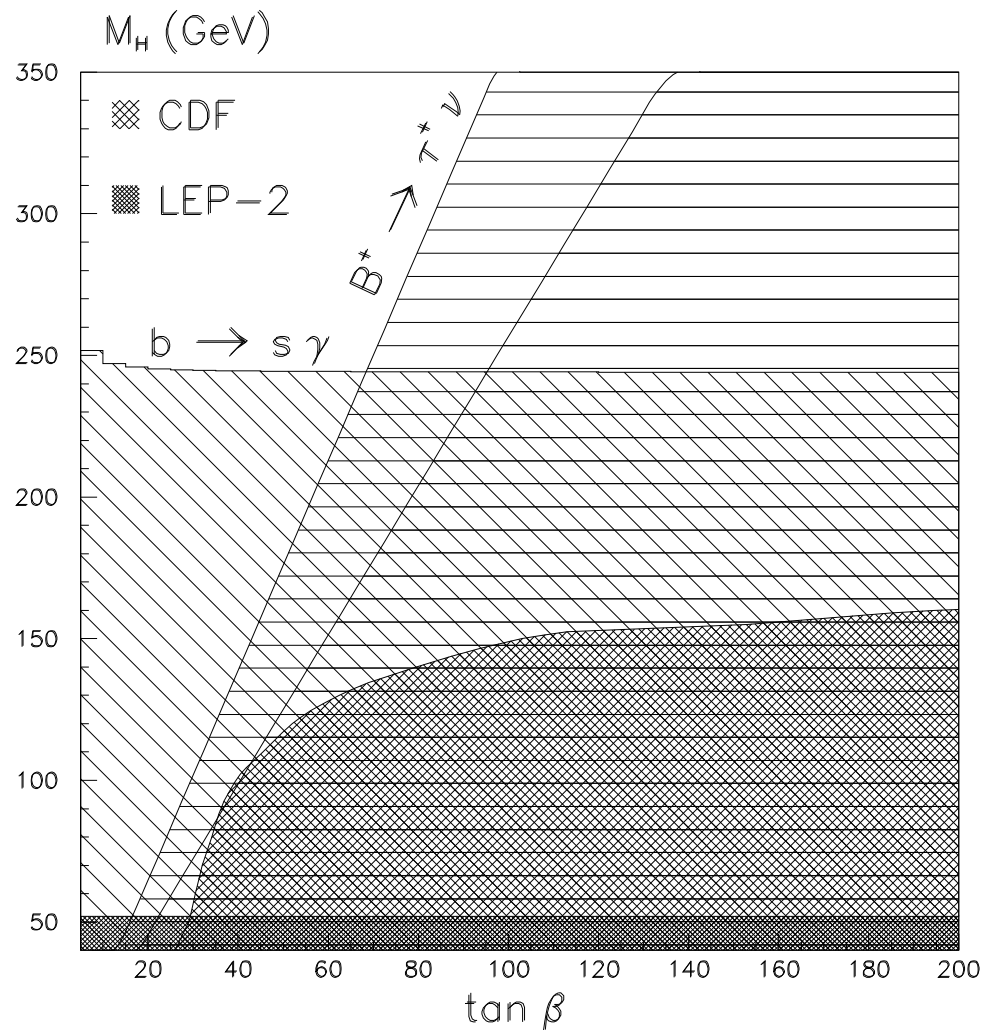
→ slightly better than original L3 analysis (0.38)

→ better than original Hou '92 (0.52)

right line: L3 original ($\tan \beta \leq 0.38 m_{H^-} / 1\text{GeV}$)

left line: Mangano/Slabopitsky very optimistic: $\tan \beta \leq 0.27 m_{H^-} / 1\text{GeV}$

Hou limit would be almost exactly diagonal. (NB: flipped w.r.t. my plots)



Mangano/Slabopitsky 97

What does the $B_u \rightarrow \tau\nu$ measurement change ?

- We now have a measurement of $B_u \rightarrow \tau\nu$ from the B factories, therefore L3 result not interesting anymore for $\tan\beta/M_H$ -limits
- But: $B_{u/c} \rightarrow \tau\nu$ at Z peak still interesting ?
- What does L3 (or any other experiment at the Z peak) actually measure ?

$$\text{BR}_{\text{eff}} = \text{BR}(B^\pm \rightarrow \tau^\pm\nu) \left(1 + \frac{N_c}{N_u}\right)$$

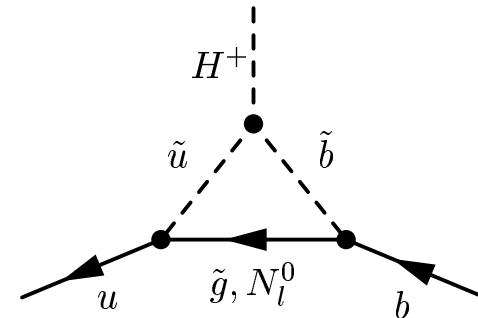
$$\frac{N_c}{N_u} = \left| \frac{V_{cb}}{V_{ub}} \right|^2 \frac{F_{b \rightarrow B_c^\pm}}{F_{b \rightarrow B^\pm}} \left(\frac{f_{B_c}}{f_B} \right)^2 \frac{M_{B_c} \tau_{B_c}}{M_B \tau_B} = 0.35 - 1.0 \cdot \frac{F_{b \rightarrow B_c}}{10^{-3}}$$

→ For $F_{b \rightarrow B_c} \sim 10^{-3}$, there can be one B_c event for each B_u event!

Significant B_c contribution to $B \rightarrow \tau\nu$ at Z peak!

- There is a surprisingly large number of $B_c^+ \rightarrow \tau^+ \nu$ in the $B^+ \rightarrow \tau^+ \nu$ signal at the Z peak!

- Also important: “ ϵ -corrections”:



- Different corrections for B_u and B_c are possible, important to know both $B_u^+ \rightarrow \tau^+ \nu$ and $B_c^+ \rightarrow \tau^+ \nu$ rate !
- If SM is assumed: Use Z peak measurement to determine $F_{b \rightarrow B_c}$!
 → Understand B_c production

Conclusions ($B \rightarrow \tau\nu$)

- $B \rightarrow \tau\nu$ is a very interesting decay channel, small in the SM, strongly modified by New Physics
- 2HDMs modify $B \rightarrow \tau\nu \Rightarrow B \rightarrow \tau\nu$ constrains 2HDMs (and other NP models)
- Very good complementarity between $\Upsilon(4S)$ and Z peak ($B_c \rightarrow \tau\nu$) !
- Need to know both channels (ϵ -corrections)
- Please measure $B \rightarrow \mu\nu$! BaBar's limit is 30% better ...

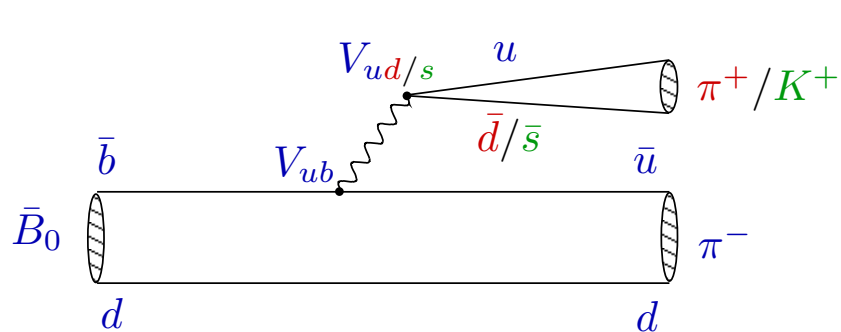
$$B \rightarrow \pi K$$

Why $B \rightarrow \pi K$?

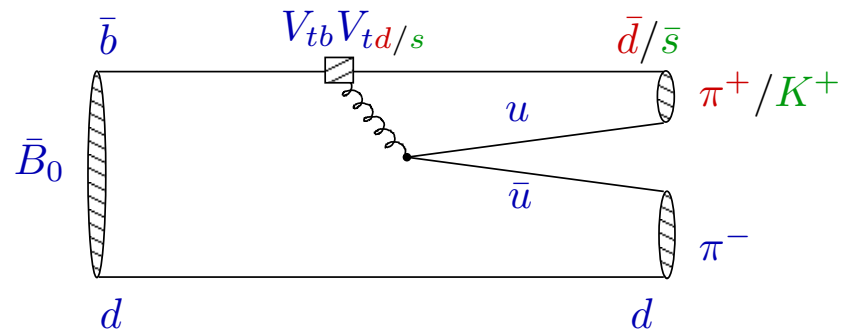
The thing that intrigued the theorists:

- Those observables that had small electroweak (EW) contributions were as expected
- Observables with large EW corrections did not agree with expectations
- EW sector is where new physics would be expected !

Feynman diagrams for $B \rightarrow \pi\pi$, $B \rightarrow \pi K$



tree diagram

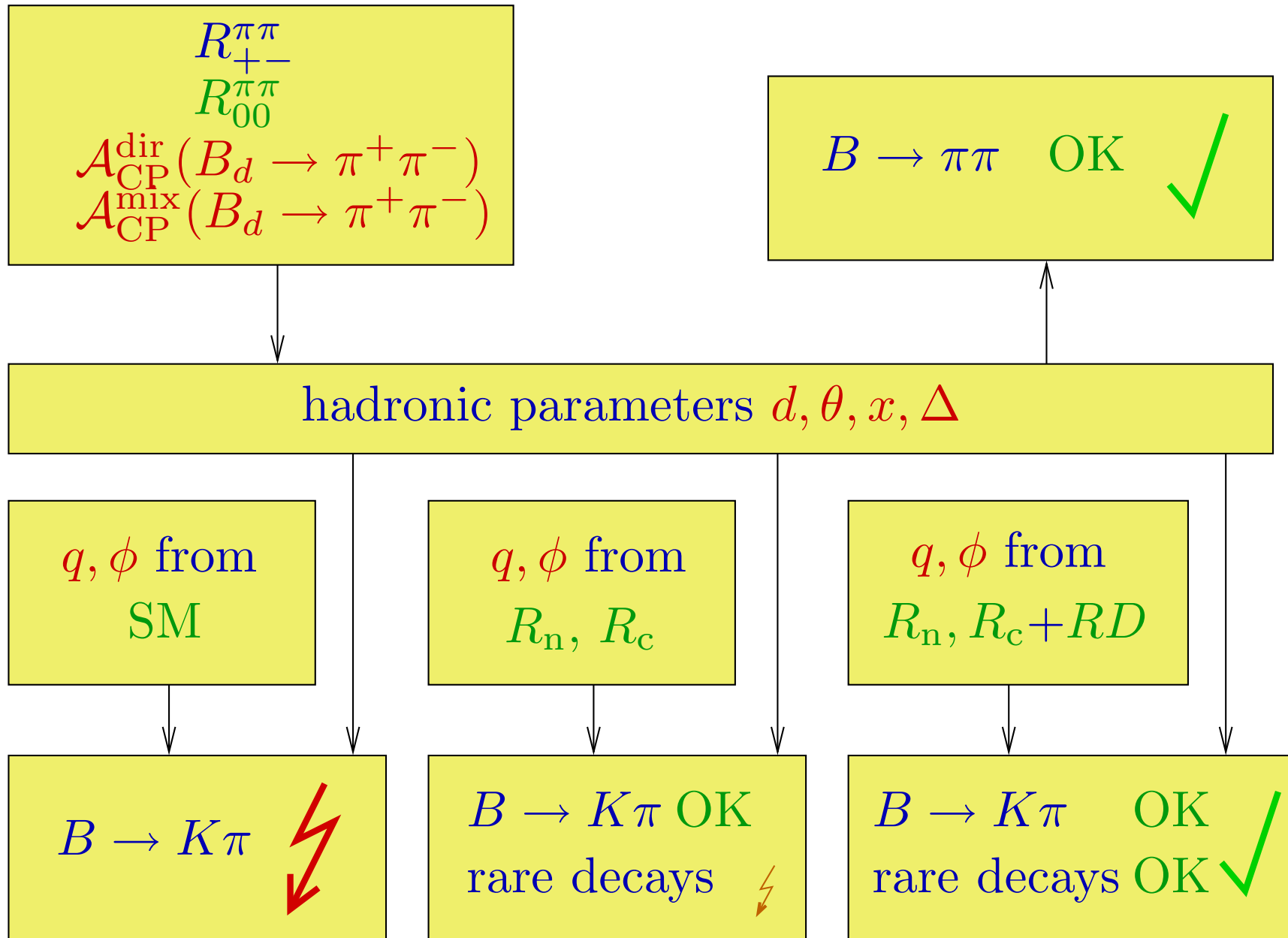


penguin diagram

Colour-suppressed tree diagrams have the same topology as the QCD penguin diagrams, electroweak penguin diagrams have the same topology as tree diagrams.

$$(P/T)_{K\pi} / (P/T)_{\pi\pi} \sim (V_{cs}/V_{us}) / (V_{cd}/V_{ud})_{\pi\pi} \sim 1/\lambda^2.$$

$\implies B \rightarrow \pi\pi$ is tree-dominated, $B \rightarrow K\pi$ is penguin-dominated.



The approach:

i) *$SU(3)$ flavour symmetry*

$SU(3)$ -breaking effects are, however, included through ratios of decay constants and form factors. Also: sensitivity of the numerical results on non-factorizable $SU(3)$ -breaking effects is explored.

ii) *Neglect of the penguin annihilation and exchange topologies*

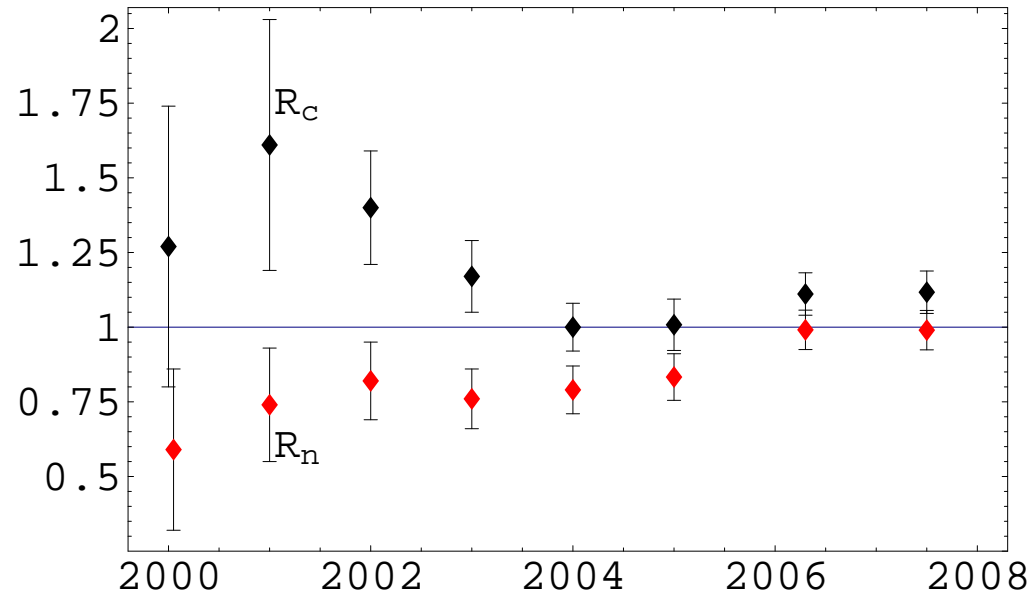
Strategy:

i) Use experimental data on BRs and asymmetries in $B \rightarrow \pi\pi$ to determine $\pi\pi$ hadronic parameters

ii) With $SU(3)$, transform these to πK hadronic parameters

iii) Calculate all πK observables, compare with experiment

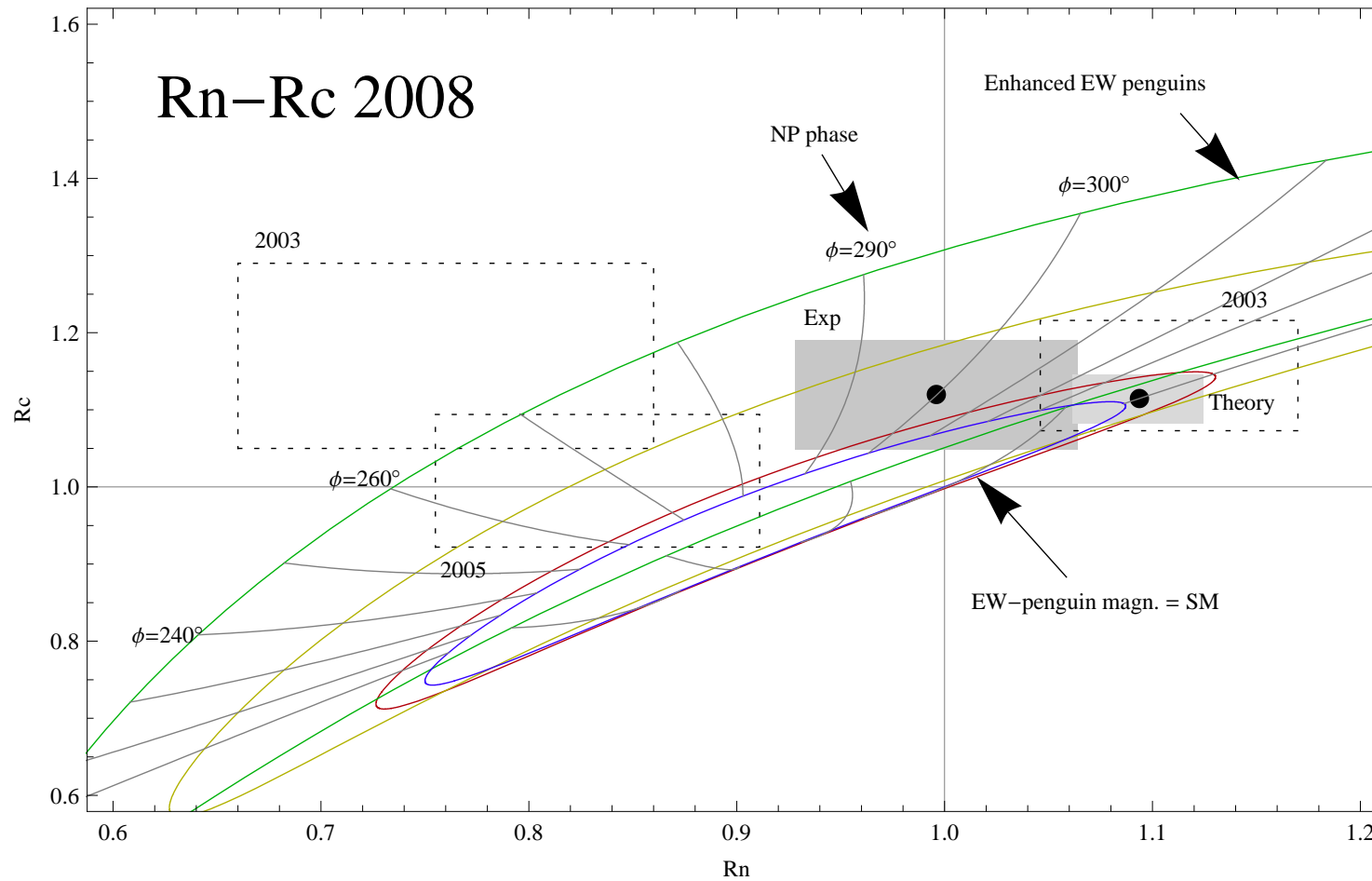
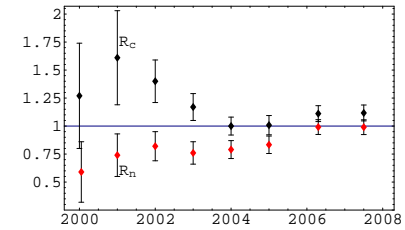
The $B \rightarrow \pi K$ puzzle has been around for a while, already in 2000 it was observed that the CLEO data exhibited a puzzling pattern.



$$R_c \equiv 2 \left[\frac{\text{BR}(B^\pm \rightarrow \pi^0 K^\pm)}{\text{BR}(B^\pm \rightarrow \pi^\pm K^0)} \right] \quad R_n \equiv \frac{1}{2} \left[\frac{\text{BR}(B_d \rightarrow \pi^\mp K^\pm)}{\text{BR}(B_d \rightarrow \pi^0 K^0)} \right]$$

The first $B \rightarrow \pi K$ puzzle was the R_c - R_n puzzle.

Situation in the R_c and R_n plane:

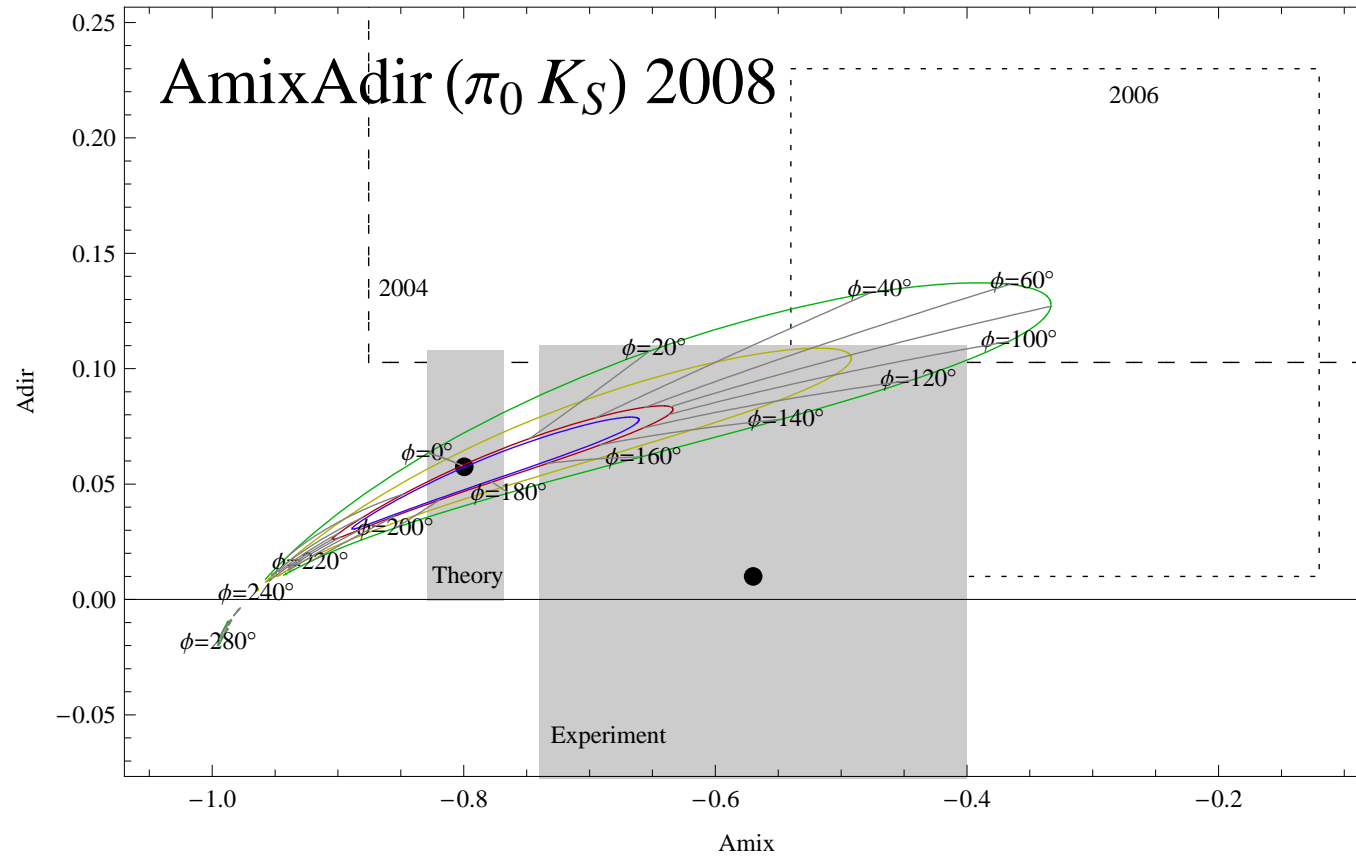


Experimental data has moved towards theory, no more puzzle.

Later (~ 2006):

R_c - R_n puzzle almost solved, but some asymmetries still puzzling.

E.g.: $\mathcal{A}_{\text{CP}}^{\text{mix}}(B_d \rightarrow \pi^0 K_S)$ predicted ~ -0.9 but experiment ~ -0.3 .



Also (almost) resolved, both theory and experiment have moved !

($\Delta A \equiv \mathcal{A}_{\text{CP}}^{\text{dir}}(B^\pm \rightarrow \pi^0 K^\pm) - \mathcal{A}_{\text{CP}}^{\text{dir}}(B_d \rightarrow \pi^\mp K^\pm) \neq 0$ is a hadronic effect.)

Conclusions ($B \rightarrow \pi K$ puzzle)

- $B \rightarrow \pi K$ is very interesting because (unlike $B \rightarrow \pi\pi$) it is penguin dominated (\rightarrow room for New Physics)
- People were excited about the $B \rightarrow \pi K$ puzzle because the observables with large EW contributions (where new physics would be expected) were peculiar. Also, QCD factorisation does not work as well as originally assumed.
- Improved experimental data and improved theory now give a consistent picture.