

# Semileptonic (and leptonic) B decays

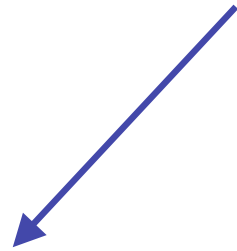
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Austrian Academy of Sciences*



1<sup>st</sup> open meeting of the  
SuperKEKB collaboration

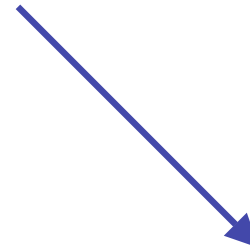
December 10-12, 2008  
KEK, Japan

# Semileptonic/leptonic decays



precision  
measurements  
of  $|V_{cb}|$  and  $|V_{ub}|$

①



rare decays,  
search for new  
phenomena

②

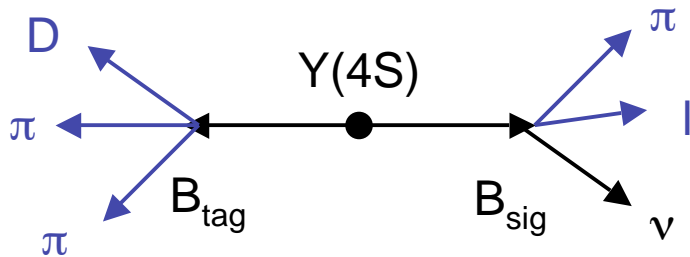
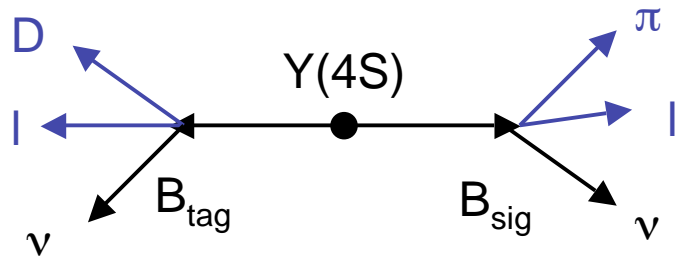
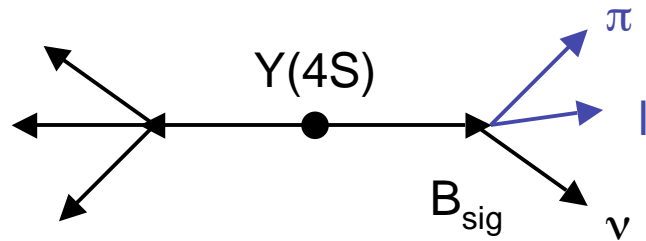
# ① Current precision

	$ V_{cbl} $	$ V_{ubl} $
exclusive	~3%	~16%
inclusive	~2%	~7%

Specific final states

All final states within a given region of phase space

# Tagging



## Untagged

- Only signal reconstructed
- High efficiency

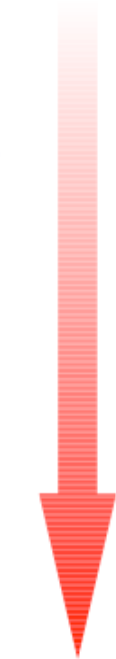
## Semileptonic tag

- Good statistics, clean events
- Kinematics not fully reconstructed

## Fullrecon tag

- Kinematics fully known
- Low statistics

Efficiency



Purity

# $|V_{cb}|$ from $B^0 \rightarrow D^{(*)} \ell \bar{\nu}_\ell$

- Decay width

$$\frac{d\Gamma}{dw}(\bar{B} \rightarrow D^* \ell \bar{\nu}_\ell) = \frac{G_F^2}{48\pi^3} |V_{cb}|^2 m_{D^*}^3 (w^2 - 1)^{1/2} P(w) (\mathcal{F}(w))^2$$

$$\frac{d\Gamma}{dw}(\bar{B} \rightarrow D \ell \bar{\nu}_\ell) =$$

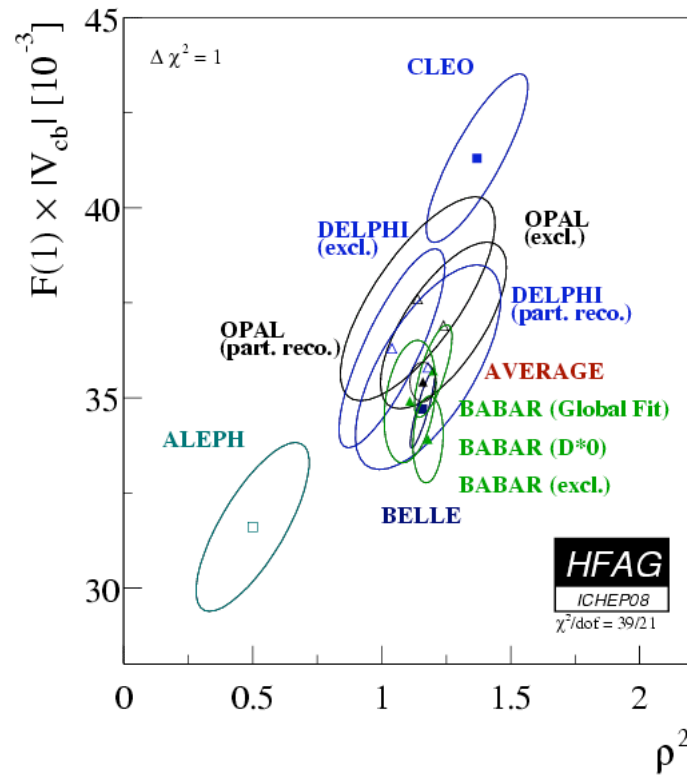
$$\frac{G_F^2}{48\pi^3} |V_{cb}|^2 (m_B + m_D)^2 m_D^3 (w^2 - 1)^{3/2} (\mathcal{G}(w))^2 \quad w \equiv v \cdot v'$$

form factor

- Experiments fit  $F(1)|V_{cb}|$  and  $G(1)|V_{cb}|$  using a form factor parameterization based on HQET and dispersion relations [Caprini et al., Nucl. Phys. B530, 153 (1998)]
- Form factor normalizations from lattice QCD

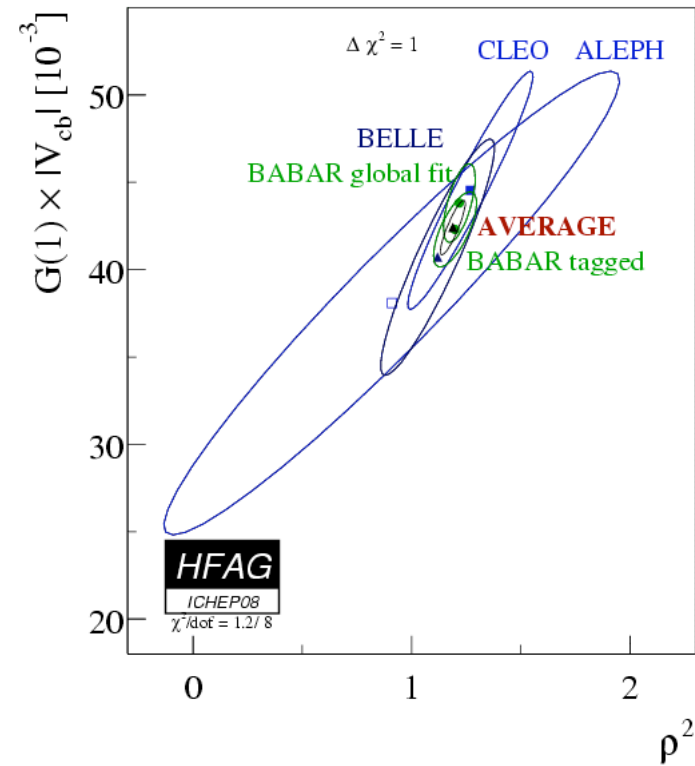
$F(1) = 0.921 \pm 0.013 \pm 0.020$	J.Laiho et al. [arXiv:0808.2519]
$G(1) = 1.074 \pm 0.018 \pm 0.016$	M.Okamoto et al. [Nucl.Phys.Proc.Suppl. 140, 461 (2005)]

D\*



1.6%

D



2.4%

$ V_{cb}  = (38.1 \pm 0.6(\text{exp}) \pm 0.9(\text{th})) \times 10^{-3} \text{ (D}^*)$
$ V_{cb}  = (39.7 \pm 1.4(\text{exp}) \pm 0.9(\text{th})) \times 10^{-3} \text{ (D)}$

3.5%

2.3%

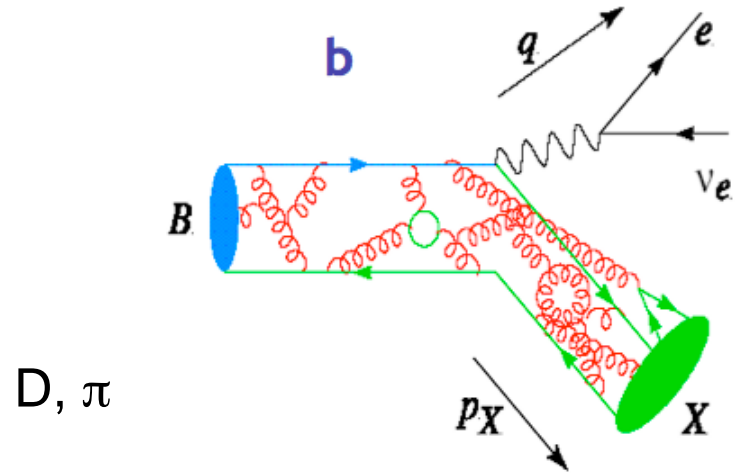
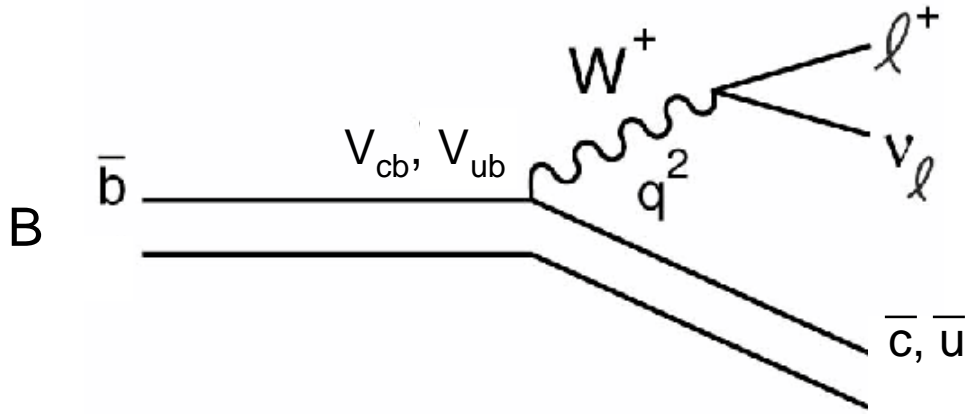
# Belle $B^0 \rightarrow D^{*+} \ell^+ \nu$ untagged

Breakdown of the systematic error components

	$\rho^2$	$R_1(1)$	$R_2(1)$	$\mathcal{B}(B^0)$	$\mathcal{F}(1)  V_{cb} $
Stat. error	0.050	0.060	0.043	0.030	0.22
$D^{**}$	0.015	0.038	0.011	0.051	0.25
Uncorr.	0.009	0.028	0.002	0.003	0.04
Sig.corr.	0.003	0.003	0.007	0.028	0.14
Fake $\ell$	0.020	0.037	0.009	0.002	0.04
Fake $D^*$	0.012	0.011	0.009	0.034	0.33
Continuum	0.003	0.008	0.000	0.001	0.02
Trk., det.eff.	-	-	-	0.221	0.86
$\mathcal{B}(D^0)$	-	-	-	0.081	0.31
$\mathcal{B}(D^*)$	-	-	-	0.033	0.13
$B^0$ life time	-	-	-	0.026	0.10
$N_{B\bar{B}}$	-	-	-	0.036	0.14
$f_{+-}/f_{0\bar{0}}$	0.003	0.011	0.005	0.001	0.04
Syst. error	0.029	0.062	0.019	0.251	1.04

[arXiv:0810.1657]

# $|V_{cb}|$ from $B \rightarrow X_c l \nu$



- $\Gamma(B \rightarrow X_c l \nu)$  can be systematically calculated with the operator production expansion (OPE)

$$\Gamma_{\text{sl}}(b \rightarrow c) = \frac{G_F^2 m_b^5(\mu)}{192 \pi^3} |V_{cb}|^2 (1 + A_{\text{ew}}) A^{\text{pert}}(r, \mu)$$

$$\left[ z_0(r) \left( 1 - \frac{\mu_\pi^2(\mu) \mu_G^2(\mu) + \frac{\rho_D^3(\mu) \rho_{LS}^3(\mu)}{m_b(\mu)}}{2m_b^2(\mu)} \right) \right]$$

$$- 2(1-r) \left[ \frac{\mu_G^2(\mu) \frac{\rho_D^3(\mu) \rho_{LS}^3(\mu)}{m_b(\mu)}}{m_b^2(\mu)} + d(r) \frac{\rho_D^3(\mu)}{m_b^3(\mu)} + \dots \right]$$

$$r = m_c^2(\mu) / m_b^2(\mu)$$

HQ parameters (non-calculable; contain soft QCD physics)

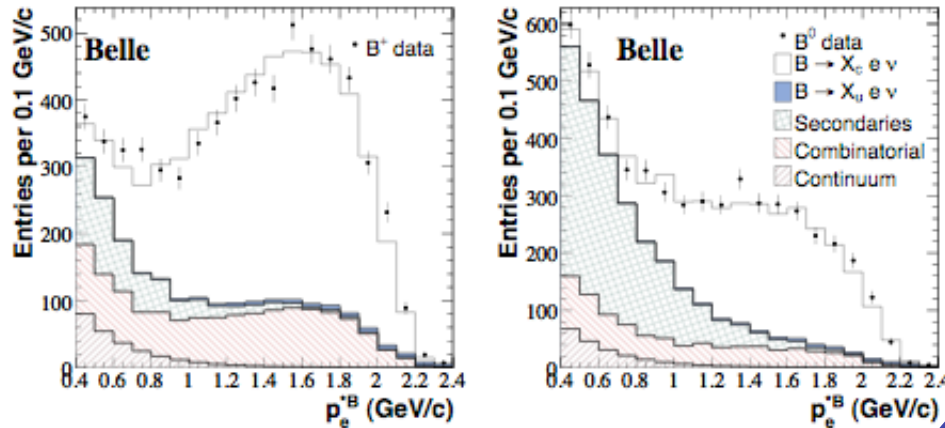
from [Benson et al., Nucl. Phys. B665, 367 (2003)]



- Non-perturbative parameters can be **measured** from inclusive observables in B decays

### Inclusive $E_1$ spectrum

[Phys.Rev. D75, 032001 (2007)]



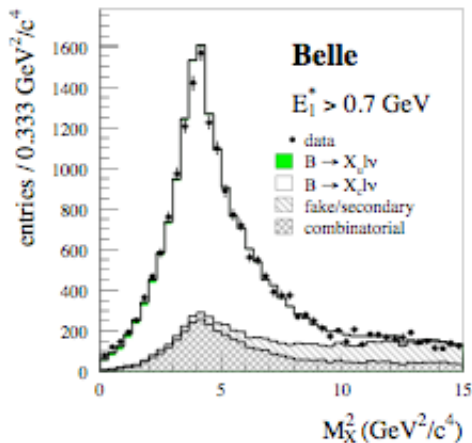
rate

shape

$|V_{cb}|$  at 1-2%

### Inclusive $M^2_X$ spectrum

[Phys.Rev. D75, 032005 (2007)]



shape

Non-perturbative parameters  
( $m_b, m_c, \mu^2_\pi, \dots$ )

shape



$B \rightarrow X_s \gamma$

[Phys.Rev. D78, 032016 (2008)]



[Phys.Rev. D78, 032016 (2008)]

## Kinetic scheme ( $X_c l \nu + X_s \gamma$ data)

$$|V_{cb}| = (41.58 \pm 0.69_{\text{fit}} \pm 0.08_{\tau_B} \pm 0.58_{\text{th}}) \times 10^{-3}$$
$$m_b^{\text{kin}} = 4.543 \pm 0.075 \text{ GeV}$$
$$m_c^{\text{kin}} = 1.055 \pm 0.118 \text{ GeV}$$

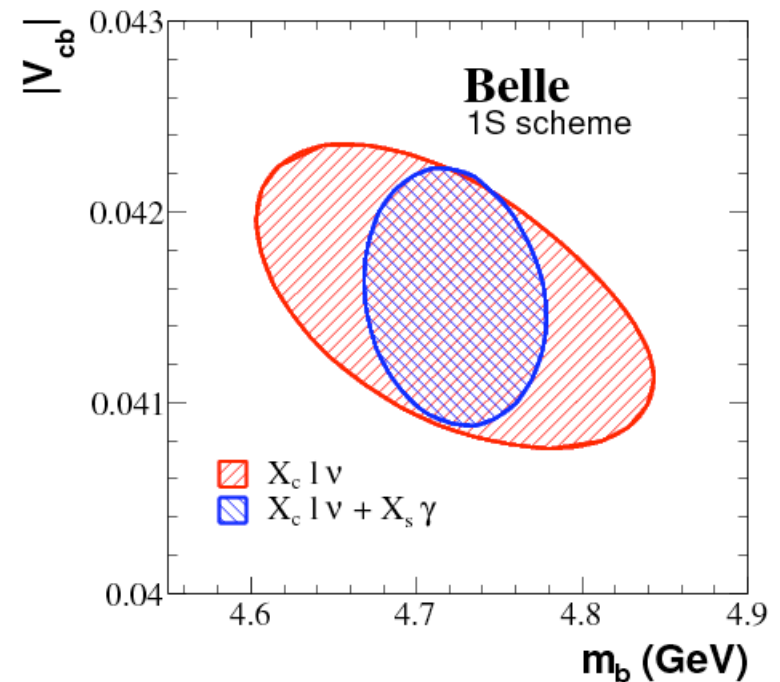
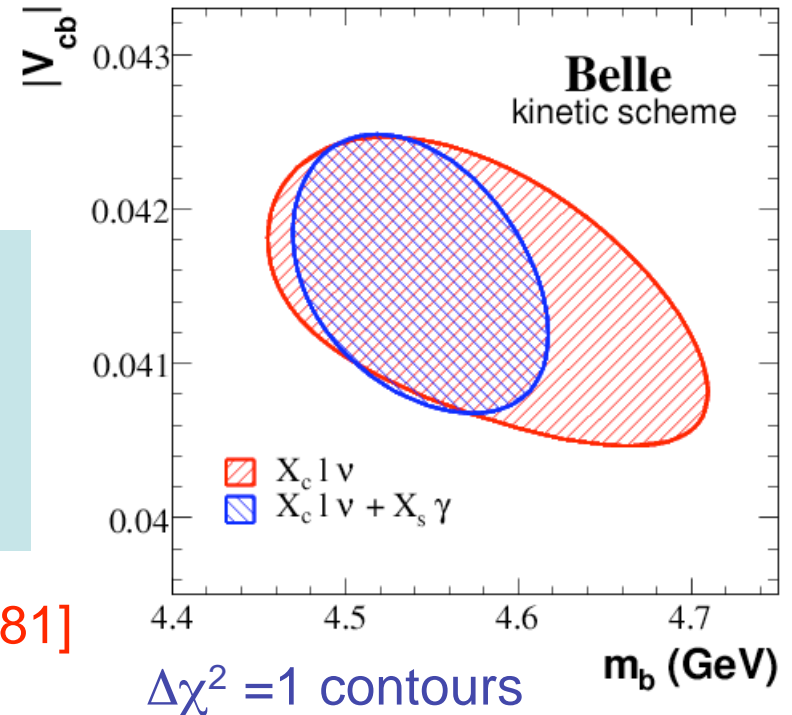
[P.Gambino, N.Uraltsev, Eur.Phys.J. C34, 181]

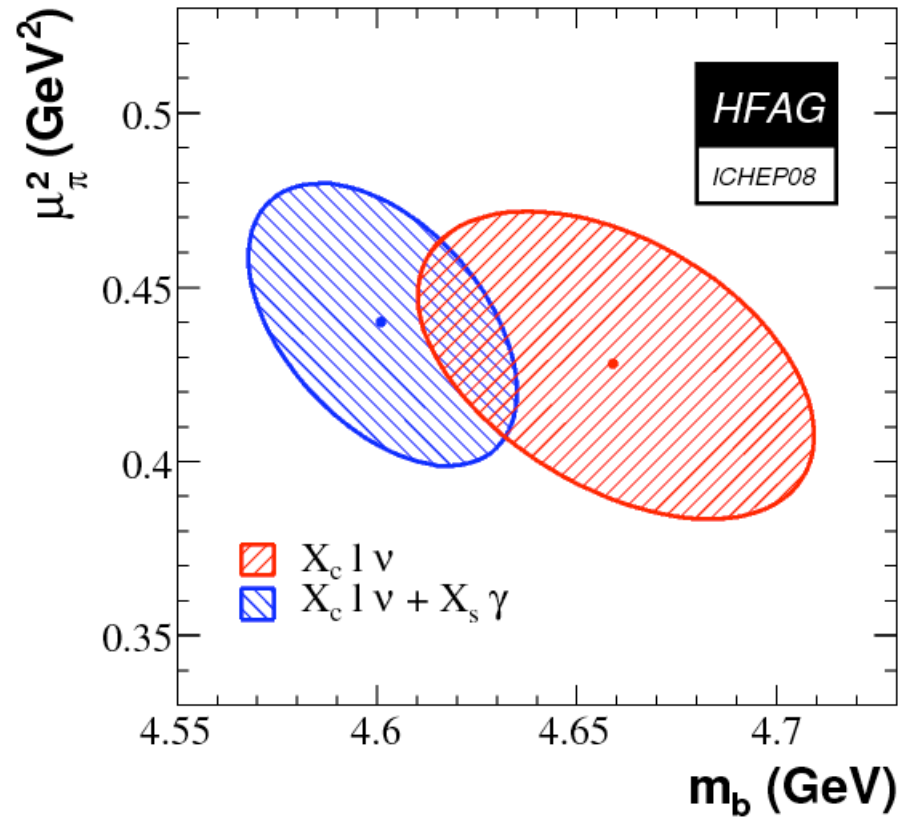
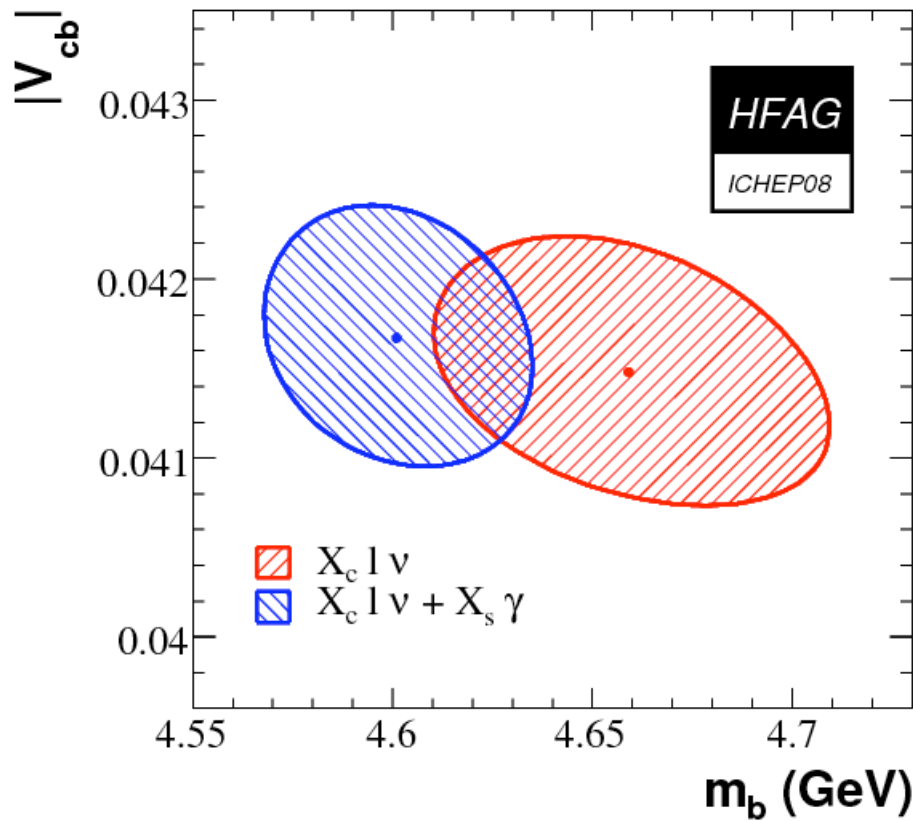
Results for  $m_b$  compatible after  
scheme translation

## 1S scheme ( $X_c l \nu + X_s \gamma$ data)

$$|V_{cb}| = (41.56 \pm 0.68_{\text{fit}} \pm 0.08_{\tau_B}) \times 10^{-3}$$
$$m_b^{1S} = 4.723 \pm 0.055 \text{ GeV}$$

[C.Bauer, Z.Ligeti, M.Luke, A.Manohar,  
Phys.Rev. D70, 094017]





Input	$ V_{cb}  (10^{-3})$	$m_b$ (GeV)	$\mu_{\pi}^2$ (GeV <sup>2</sup> )	$\chi^2/\text{ndf}$	
All moments	41.67 $\pm$ 0.43(fit) $\pm$ 0.08( $\tau_B$ ) $\pm$ 0.58(th)	4.601 $\pm$ 0.034	0.440 $\pm$ 0.040	29.7/57	1.7%
$X_c l v$ only	41.48 $\pm$ 0.47(fit) $\pm$ 0.08( $\tau_B$ ) $\pm$ 0.58(th)	4.659 $\pm$ 0.049	0.428 $\pm$ 0.044	24.1/46	1.8%

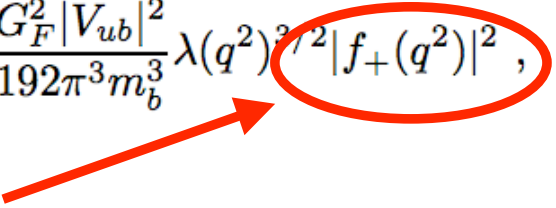
# Prospects for $|V_{cb}|$

How can we improve the measurement of  $|V_{cb}|$ ?

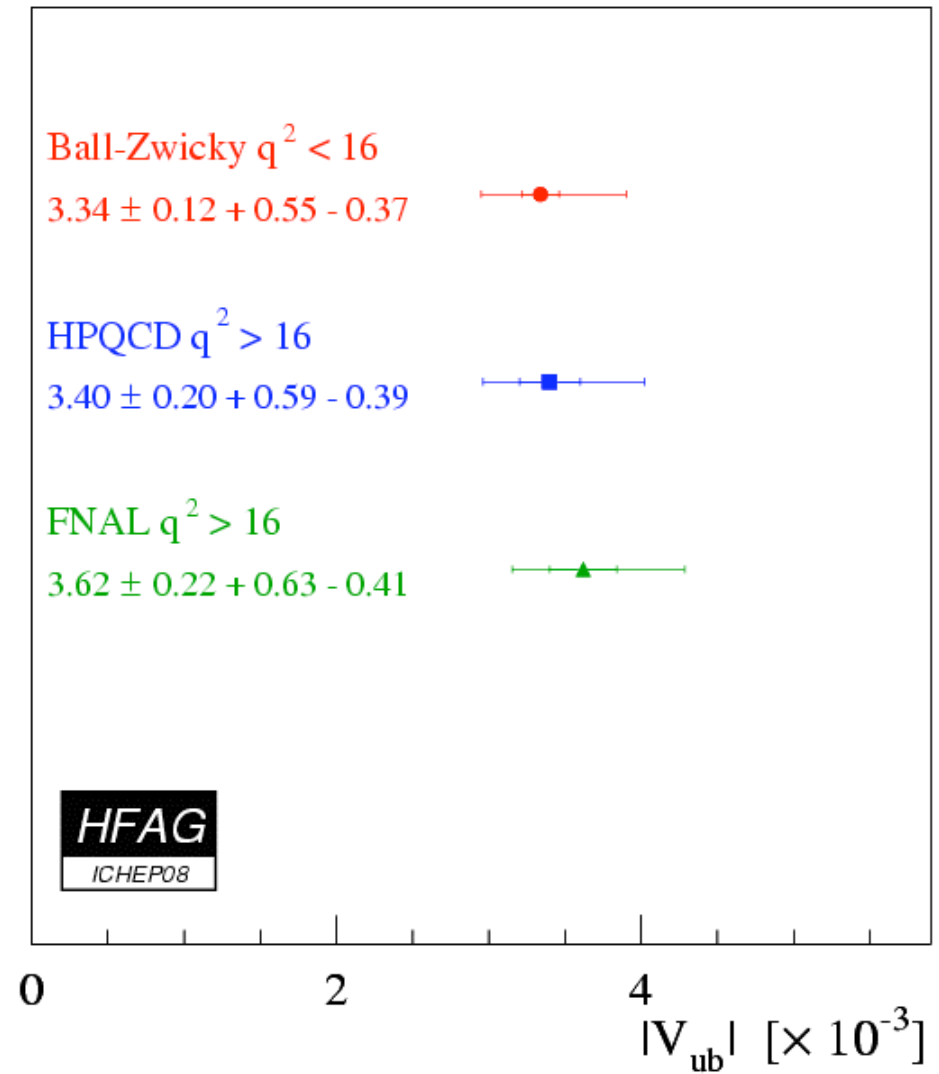
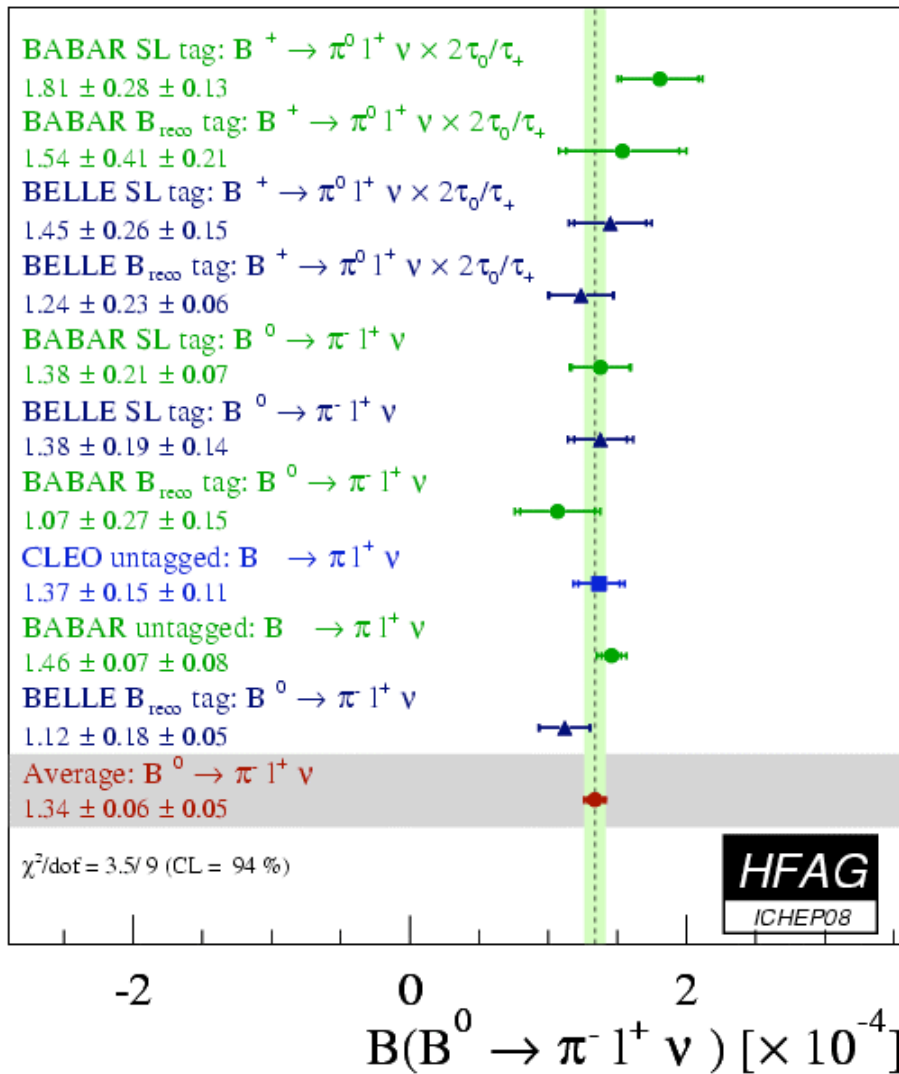
- Exclusive
  - Move to tagged measurements to reduce background systematics
  - Test assumptions of the measurement (form factor parametrization)
  - Progress in lattice QCD needed
- Inclusive
  - Current uncertainty mainly theoretical
  - Different observables might better constraint HQ parameters
  - Remove the  $B \rightarrow X_s \gamma$  data from the analysis?

# $|V_{ub}|$ from $B \rightarrow \pi \ell \nu$

- Decay width

$$\frac{d\Gamma(B \rightarrow \pi \ell \nu)}{dq^2} = \frac{G_F^2 |V_{ub}|^2}{192\pi^3 m_b^3} \lambda(q^2)^{3/2} |f_+(q^2)|^2, \quad q^2 = (p_\ell + p_\nu)^2$$


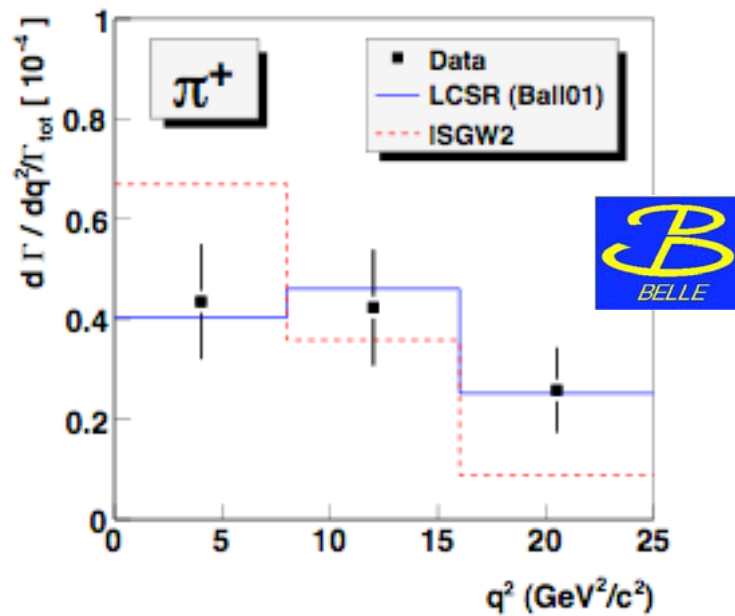
- Need form factor shape and normalization for  $|V_{ub}|$
- Available form factor calculations
  - Relativistic quark models
    - ISGW2 [Phys. Rev. D52, 2783 (1995)]
  - Light cone sum rules (LCSR) in the region  $q^2 < 14 \text{ GeV}^2$ 
    - Ball-Zwicky [Phys. Rev. D71, 014015 (2005)]
  - Lattice QCD in the region  $q^2 > 16 \text{ GeV}^2$ 
    - HPQCD [Phys. Rev. D73, 074502 (2006)]
    - FNAL [Nucl. Phys. Proc. Suppl. 140, 461 (2005)]



Experimental uncertainty ~ 4-6%  
 F.F. normalization uncertainty ~ 13-15%

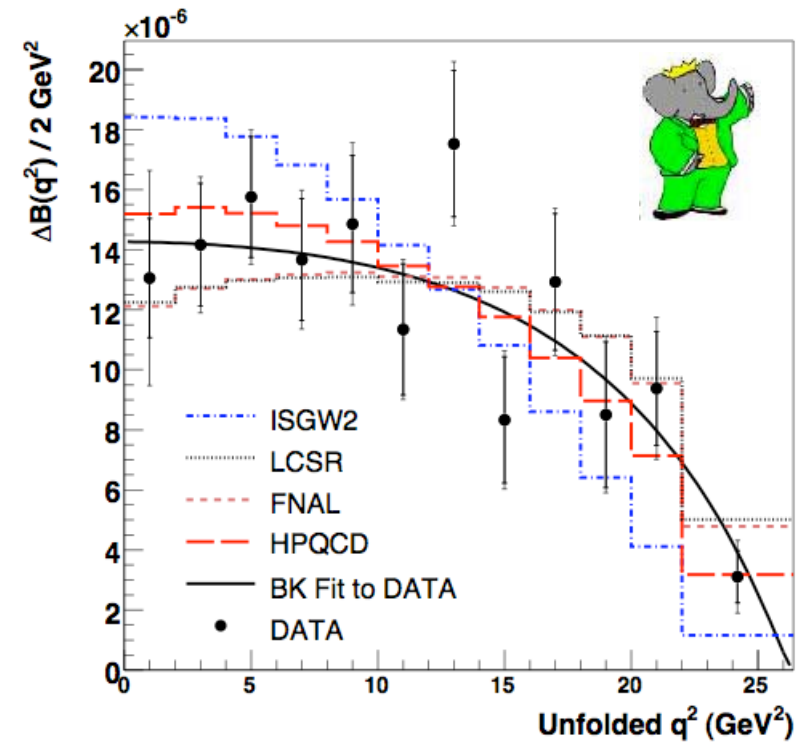
# $B^0 \rightarrow \pi^- l^+ \nu$ $q^2$ spectrum

Belle fullrecon (605/fb)



[arXiv:0812.1414]

BaBar untagged (206/fb)



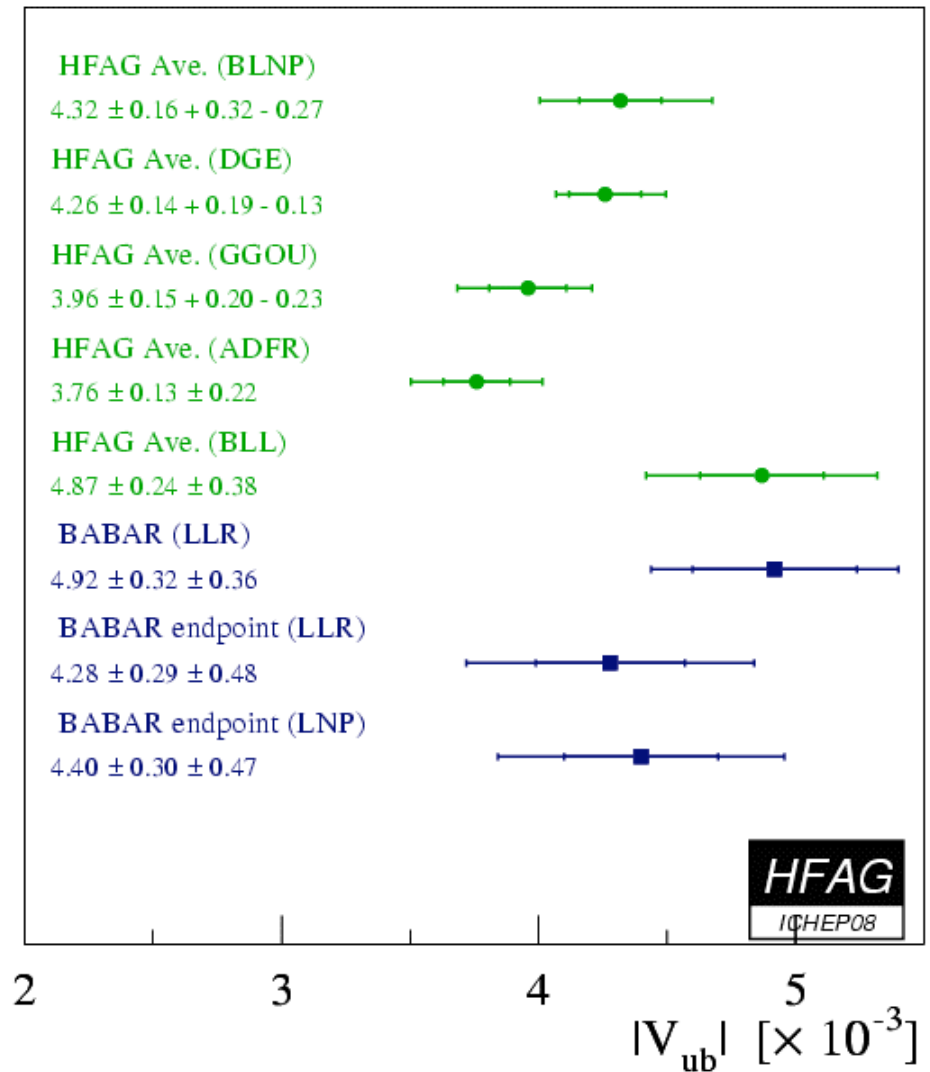
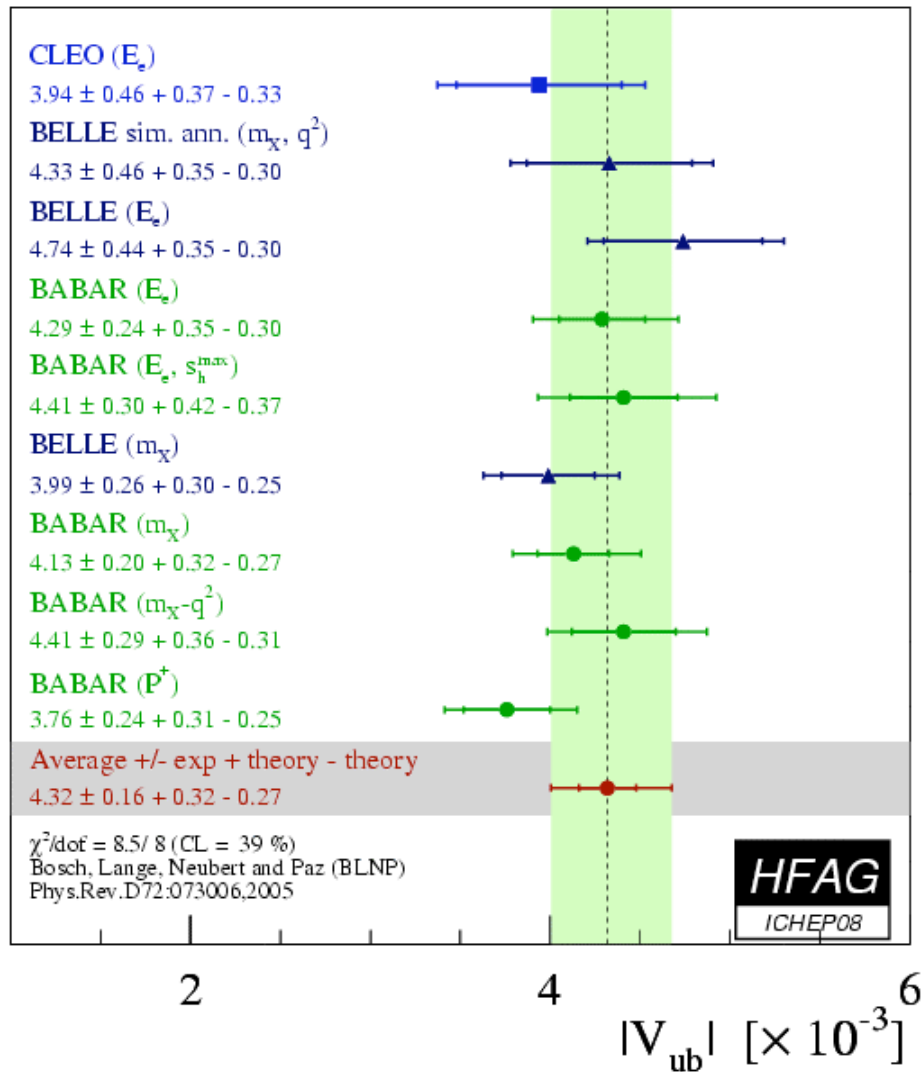
[PRL 98, 091801 (2007)]

# $|V_{ub}|$ from $B \rightarrow X_u l \nu$

- Also based on the OPE, as for  $B \rightarrow X_c l \nu$  decays
- However, experimental cuts to suppress  $X_c l \nu$  background compromise the convergence of the OPE
- Different theoretical approaches to model the non-perturbative component
  - Bosch, Lange, Neubert, Paz (BLNP) [[Phys.Rev. D72, 073006 \(2005\)](#)]
  - Anderson, Gardi (DGE) [[JHEP 0601:097 \(2006\)](#)]
  - Gambino, Giordano, Ossola, Uraltsev (GGOU) [[JHEP 0710:058 \(2007\)](#)]
  - Aglietti, Di Lodovico, Ferrera, Ricciardi (AC) [[arXiv:0711.0860](#)]
  - Bauer, Ligeti, Luke (BLL) [[Phys.Rev. D64, 113004 \(2001\)](#)]



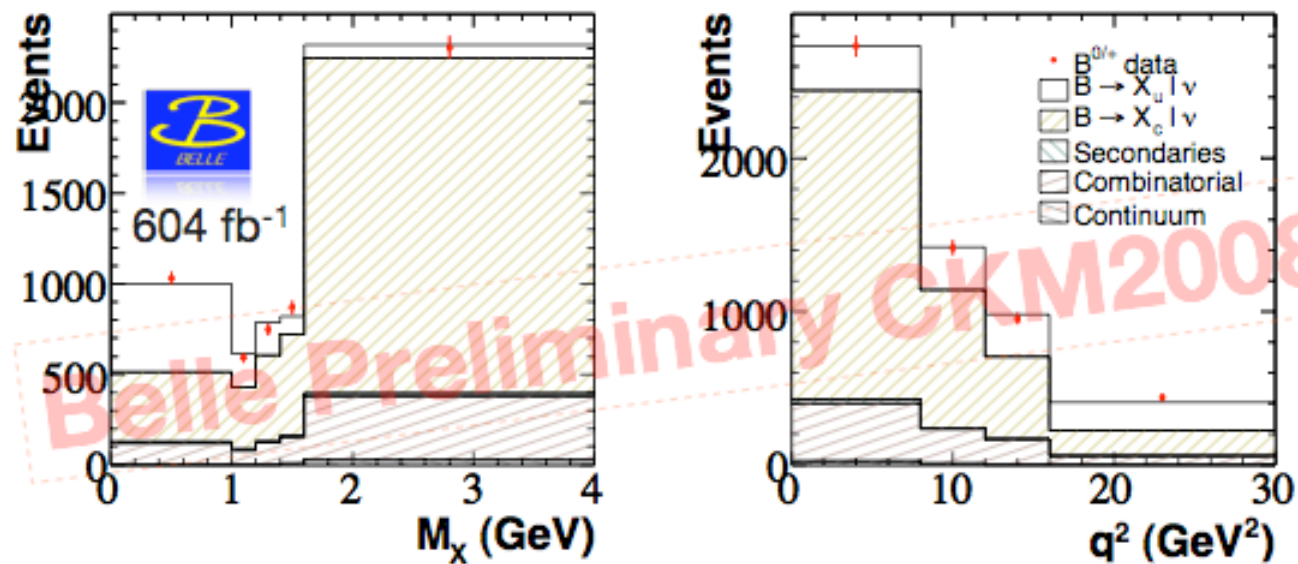
# BLNP framework



How predictive is the theory?

# Belle Multivariate analysis (NEW @ CKM2008) 2/2

Phill Urquijo



~1035 Evts

2D fit in q2 mx. (projections shown)

Kinematic Region	$B(B \rightarrow X_\nu l \nu) \times 10^{-3}$ $\Delta(\text{stat. sys.})$	$m_b$	$ V_{ub}  (10^{-3})$ % error	Theory
$P_{\text{lepton}} > 1.0$ GeV	$1.96 \times (1 \pm 0.088 \pm 0.076)$	(kinetic) 4.613 GeV, $m_{\text{up}} = 0.440 \text{ GeV}^2$	$4.42 (\pm 3.1 \pm 5.1)$	GGOU (thanks P. Giordano)
		(MSbar) 4.243 GeV	$4.47 (\pm 6.7)$	DGE (thanks E. Gardi)

~90% total phase space, thus theory error less correlated to other  $V_{ub}$  determinations

# Prospects for $|V_{ub}|$

How can we improve the measurement of  $|V_{ub}|$ ?

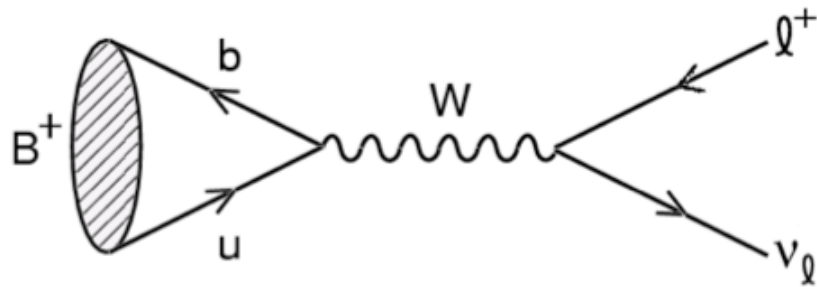
A lot of homework for theorists but...

- **Exclusive**
  - Measure (at least) the  $\pi l\nu$   $q^2$  spectrum
- **Inclusive**
  - Try to cover as much as possible of the  $X_u l\nu$  phase space

## ② Rare decays

- Leptonic decays
  - $B^+ \rightarrow l^+ \nu$  with  $l = e, \mu$  or  $\tau$
- Semi-tauonic decays
  - $B \rightarrow \bar{D}^{(*)} \tau \nu$

# Leptonic decays



helicity suppression of light leptons

$$\mathcal{B}(B^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B$$

- SM prediction with  $|V_{ub}| = (4.39 \pm 0.54) \times 10^{-3}$  and  $f_B = 189 \pm 27$  MeV

$B^+ \rightarrow e^+ \nu$	$B^+ \rightarrow \mu^+ \nu$	$B^+ \rightarrow \tau^+ \nu$
$(1.7 \pm 0.4) \times 10^{-11}$	$(7.1 \pm 1.6) \times 10^{-7}$	$(1.6 \pm 0.4) \times 10^{-4}$

- Might be enhanced due to new physics contribution (charged Higgs, ...)

- Inclusive measurements

(limits are 90% C.L.)

	$B^+ \rightarrow e^+\nu$	$B^+ \rightarrow \mu^+\nu$	$B^+ \rightarrow \tau^+\nu$
Belle [PLB647, 67]	$< 9.8 \times 10^{-7}$	$< 1.7 \times 10^{-6}$	
BaBar [arXiv:0807.4187]		$< 1.3 \times 10^{-6}$	

- Semileptonic tag






	$B^+ \rightarrow e^+\nu$	$B^+ \rightarrow \mu^+\nu$	$B^+ \rightarrow \tau^+\nu$
Belle [arXiv:0809.3834]			$(1.65 \pm 0.52) \times 10^{-4}$

- Fullrecon tag

	$B^+ \rightarrow e^+\nu$	$B^+ \rightarrow \mu^+\nu$	$B^+ \rightarrow \tau^+\nu$
Belle [PRL97, 251802]			$(1.8 \pm 0.7) \times 10^{-4}$
BaBar [PRD77, 091104; PRD77, 011107]	$< 5.2 \times 10^{-6}$	$< 5.6 \times 10^{-6}$	$(1.8 \pm 1.0) \times 10^{-4}$

# Semi-tauonic B decays

- Challenging experimentally as up to 3 neutrinos in the final state
- Fullrecon tagging is mandatory

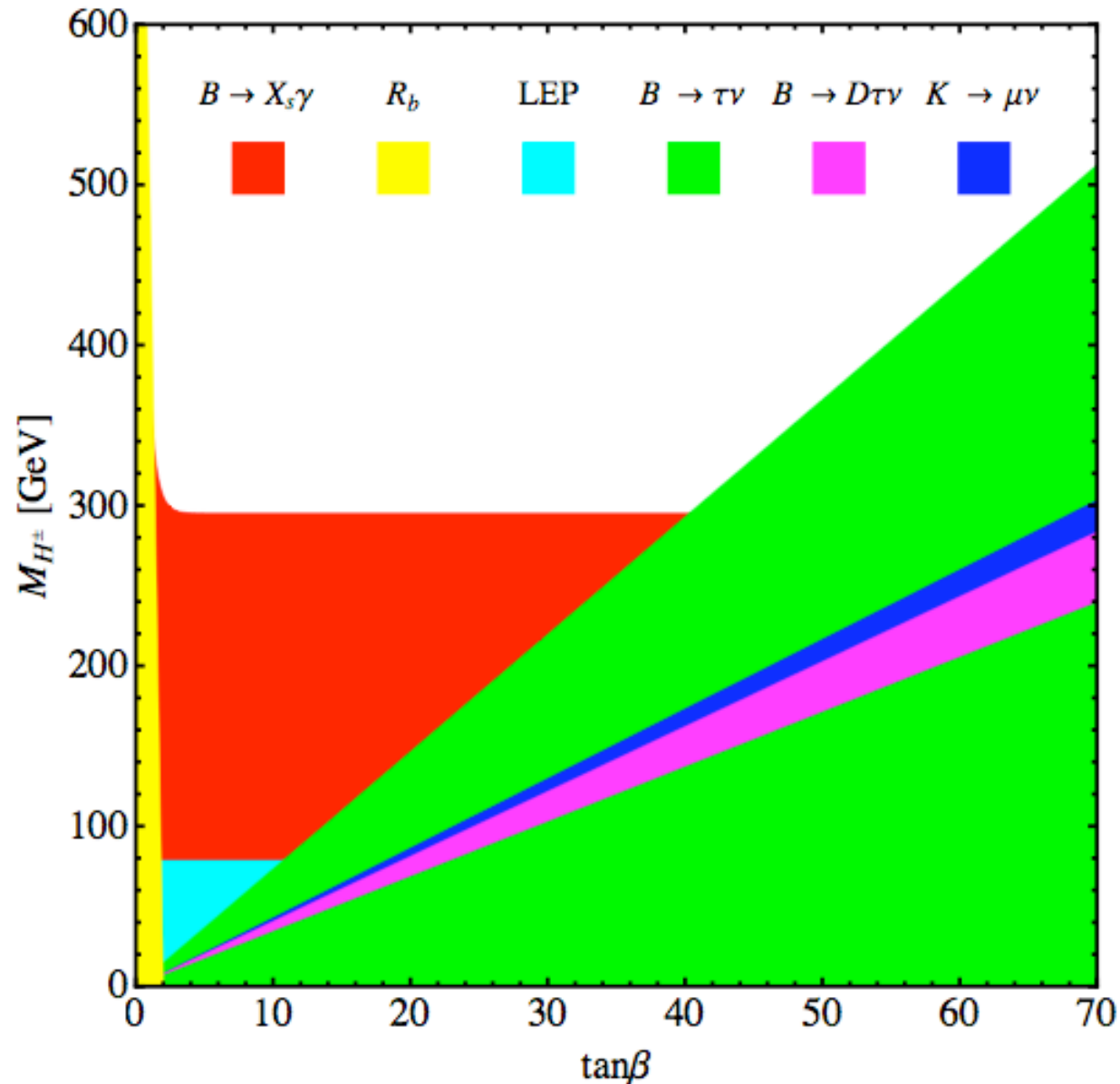
Decay mode	BF[%]	signif.	Ref.
$B^0 \rightarrow D^{*-} \tau^+ \nu_\tau$	$2.02^{+0.40}_{-0.37}(\text{stat}) \pm 0.37(\text{syst})$	$5.2\sigma$	
	$1.11 \pm 0.51(\text{stat}) \pm 0.04(\text{syst}) \pm 0.04(\text{norm})$	$2.7\sigma$	
$B^- \rightarrow D^{*0} \tau^+ \nu_\tau$	$2.25 \pm 0.48(\text{stat}) \pm 0.22(\text{syst}) \pm 0.17(\text{norm})$	$5.3\sigma$	
$B^0 \rightarrow \bar{D}^0 \tau^+ \nu_\tau$	$1.04 \pm 0.35(\text{stat}) \pm 0.15(\text{syst}) \pm 0.10(\text{norm})$	$3.3\sigma$	
$B^- \rightarrow D^0 \tau^+ \nu_\tau$	$0.67 \pm 0.37(\text{stat}) \pm 0.11(\text{syst}) \pm 0.07(\text{norm})$	$1.8\sigma$	



Belle [PRL 99, 191807 (2007)]



BaBar [PRL 100, 021801 (2008)]



Bounds on the charged Higgs mass in the 2HDM type II model as a function of  $\tan \beta$ . (Colored areas are excluded at 95% C.L.)

[U.Haisch, arXiv:0805.2141]



# Summary

- $|V_{cb}|$  and  $|V_{ub}|$ 
  - The precision of  $|V_{ub}/V_{cb}|$  can be further improved
  - Though more data alone will not suffice
- Rare (semi-)leptonic B decays
  - Sensitive probe for new physics (e.g., charged Higgs)

Backup slides

# The CKM mechanism

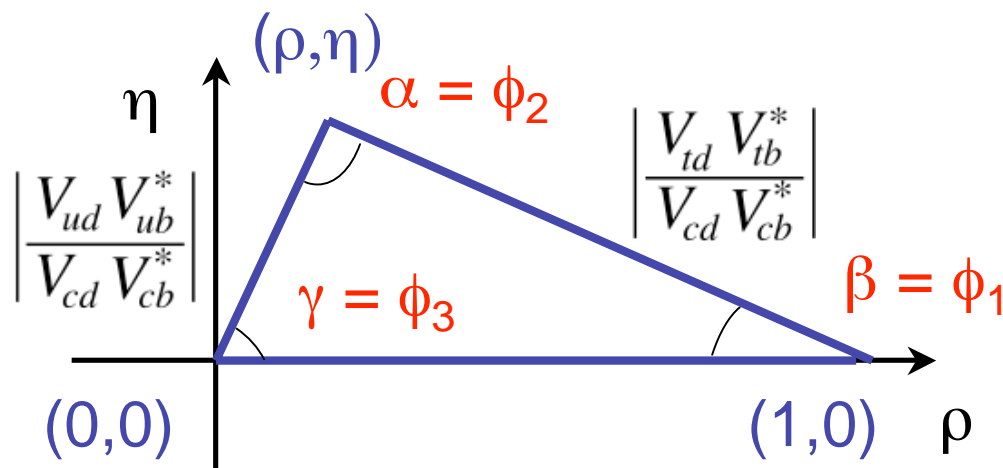
- The charged current interaction in the SM

$$-\mathcal{L}_{W^\pm} = \frac{g}{\sqrt{2}} \overline{u_{Li}} \gamma^\mu (V_{\text{CKM}})_{ij} d_{Lj} W_\mu^\pm + \text{h.c.}$$

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

[Kobayashi, Maskawa, Prog. Theor. Phys. 49, 652 (1973)]

- $V_{\text{CKM}}$  is a unitary 3x3 matrix; it contains three real parameters and one complex phase
- Its unitarity is commonly represented by the unitarity triangle



$$\alpha \equiv \phi_2 \equiv \arg \left( -\frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right)$$

$$\beta \equiv \phi_1 \equiv \arg \left( -\frac{V_{cd} V_{cb}^*}{V_{td} V_{tb}^*} \right)$$

$$\gamma \equiv \phi_3 \equiv \arg \left( -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right)$$

- At the  $Y(4S)$ ,  $B\bar{B}$  are produced at threshold
- This allows to
  - Select a B signal using two nearly independent variables

$$M_B = \sqrt{(E_{beam}^*)^2 - (\sum P_i)^2}$$

$$\Delta E = \sum E_i - E_{beam}^*$$

- Determine the 4-momentum of one B by reconstructing the other
- Distinguish  $B\bar{B}$  (spherical) from continuum events (jet-like)

