

ϕ_3 measurements



K.Trabelsi 

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sBGM, 10 Dec, 2008

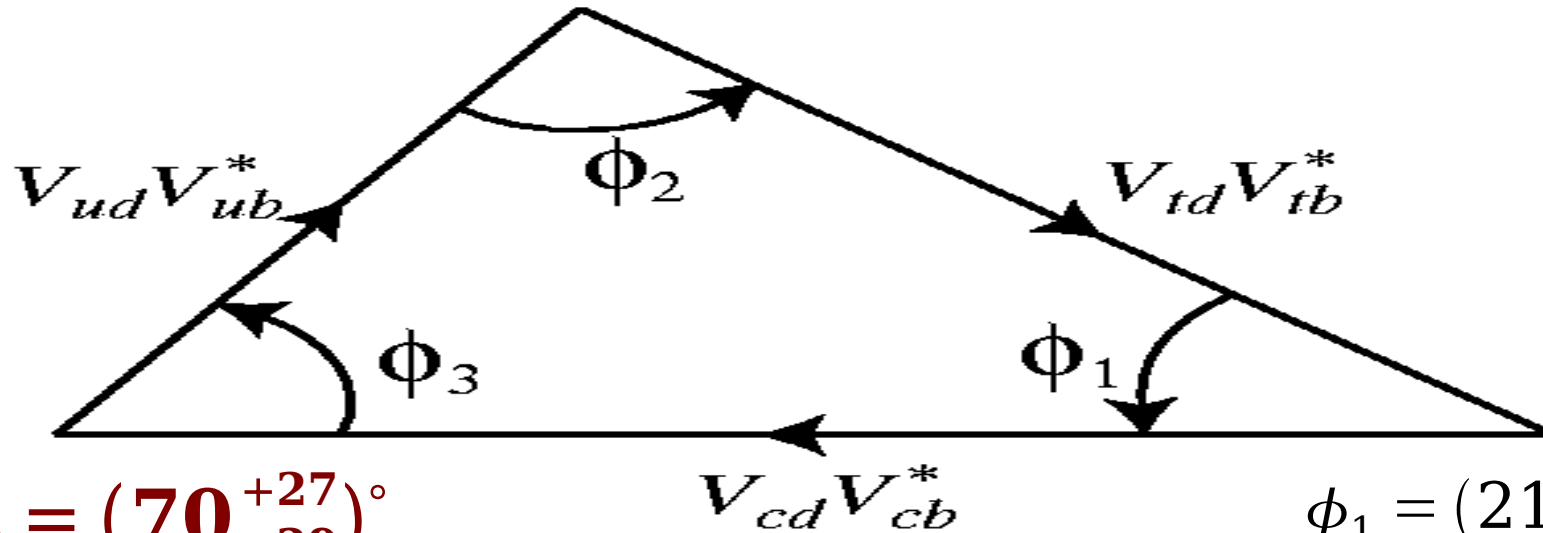
- B.Golob: use the values in the draft of the superB physics paper, i.e. 5 ab^{-1} and 50 ab^{-1} .
...(at least wherever possible) strictly divide the errors into stat., scaling and non-scaling systematics.
- T.Browder: ϕ_3 sensitivity of SuperBelle compared to LHCb

Les promesses n'engagent que ceux y croient...

News from the Unitarity Triangle

$$\phi_2 = (88.4^{+5.6}_{-4.9})^\circ$$

(WA, CKMfitter, ICHEP08)



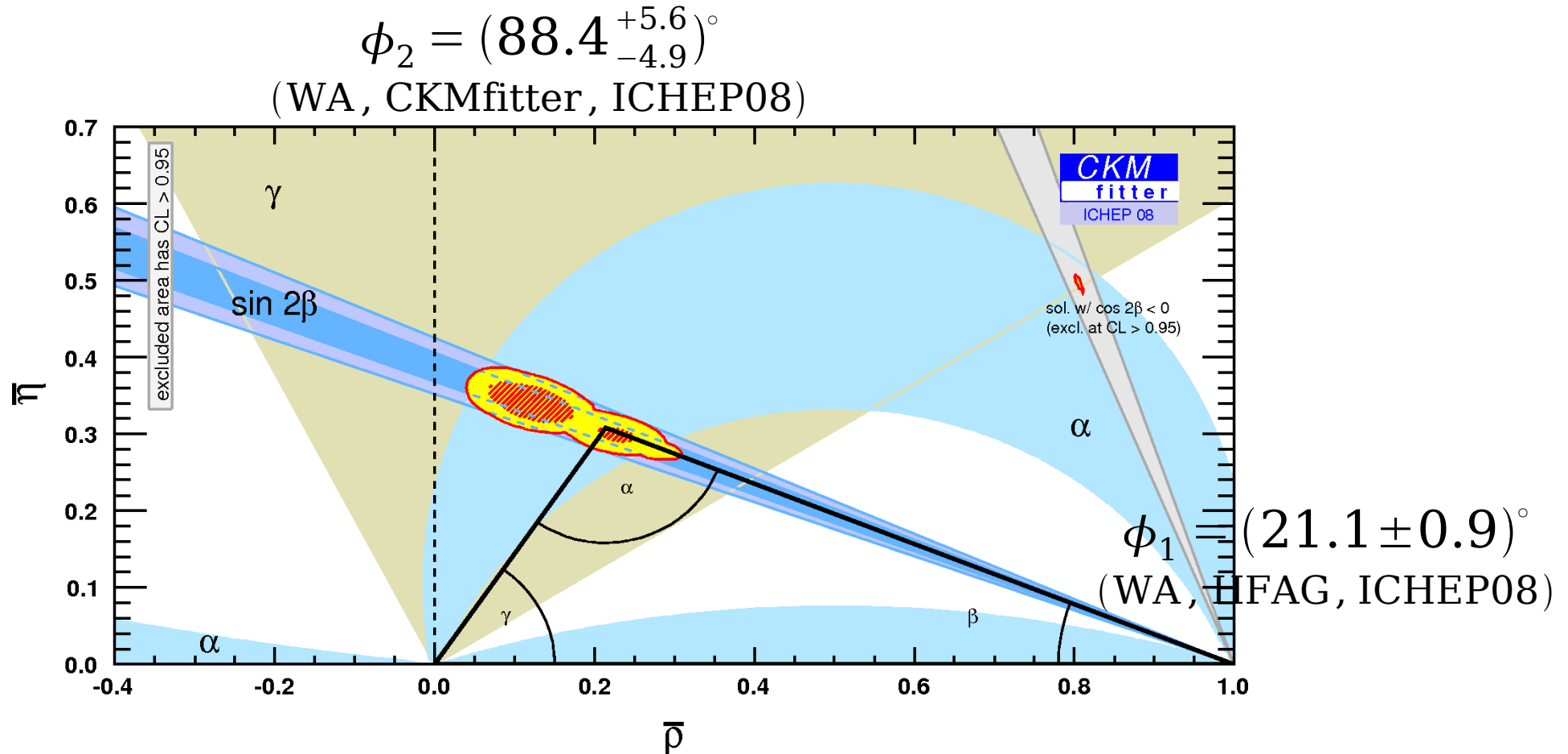
$$\phi_3 = (70^{+27}_{-29})^\circ$$

(WA, CKMfitter, CKM08)

$$\phi_1 = (21.1 \pm 0.9)^\circ$$

(WA, HFAG, ICHEP08)

News from the Unitarity Triangle



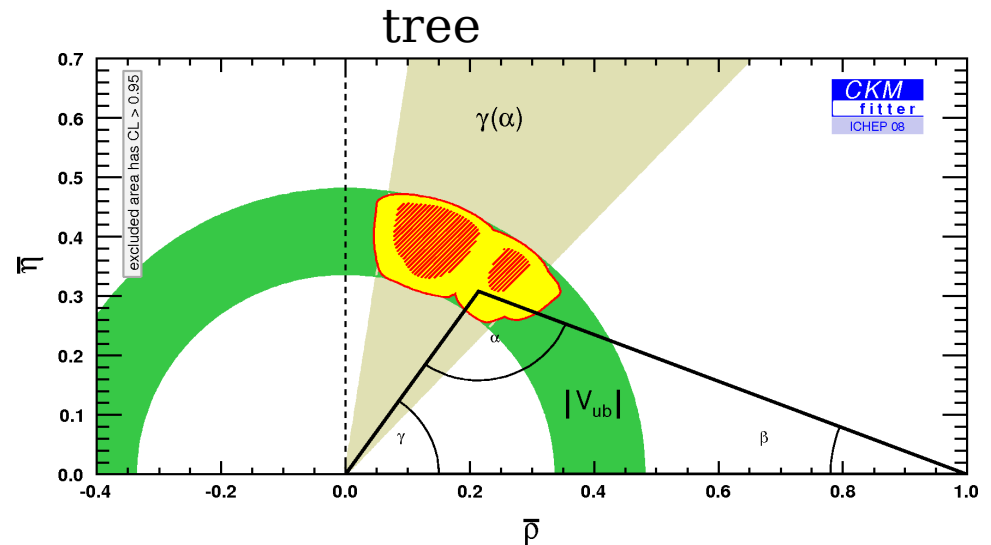
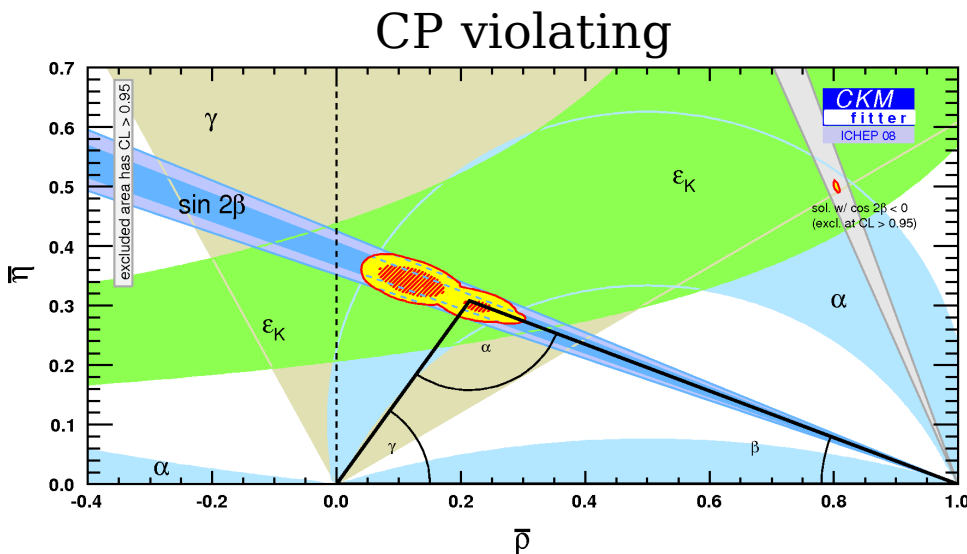
All measurements of observables sensitive to ϕ_3 are statistically limited

$$\phi_3 = (70^{+27}_{-29})^\circ \quad (\text{WA, CKMfitter, CKM08})$$

Although not all the statistics yet analyzed by Belle

Motivations

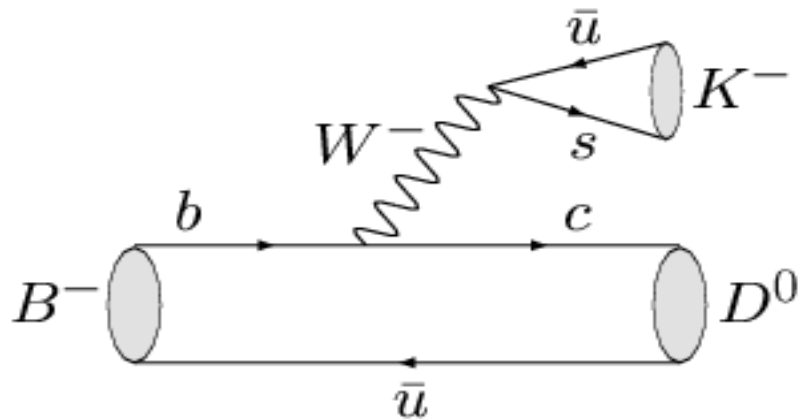
- Overconstrain the CKM matrix: measure fundamental parameters, constrain new physics effects
- Measure the 4 free parameters in various ways:
 - CP conserving $\{|V_{us}|, |V_{cb}|, |V_{td}|, |V_{ub}|\}$
 - CP violating $\{\epsilon_K, \phi_s, \phi_1, \phi_3\}$
 - Tree level $\{\dots, \dots, |V_{ub}|, \phi_3\}$
 - Loop level $\{\dots, \dots, |V_{td}|, \phi_1\}$
 - ...



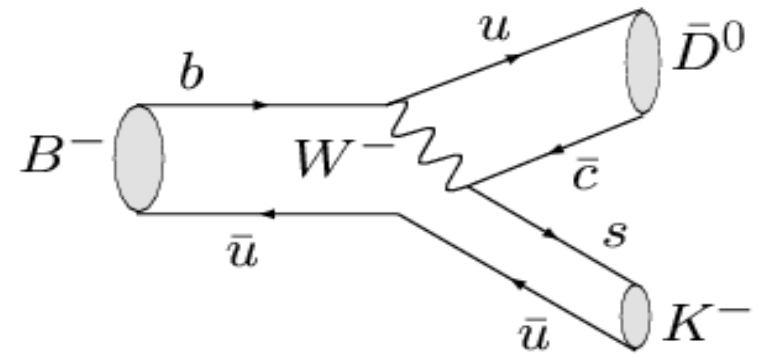
- $\sim 1\%$ seems to be the right level to test NP

γ measurements from $B^\pm \rightarrow DK^\pm$

- Theoretically pristine $B \rightarrow DK$ approach
- Access γ via interference between $B^- \rightarrow D^0 K^-$ and $B^- \rightarrow \bar{D}^0 K^-$



color allowed
 $B^- \rightarrow D^0 K^- \sim V_{cb} V_{us}^*$
 $\sim A \lambda^3$



color suppressed
 $B^- \rightarrow \bar{D}^0 K^- \sim V_{ub} V_{cs}^*$
 $\sim A \lambda^3 (\rho + i\eta)$

relative magnitude of suppressed amplitude is r_B

$$r_B = \frac{|A_{\text{suppressed}}|}{|A_{\text{favoured}}|} \sim \frac{|V_{ub} V_{cs}^*|}{|V_{cb} V_{us}^*|} \times [\text{color supp}] = 0.1 - 0.2$$

relative weak phase is ϕ_3 , relative strong phase is δ_B

γ measurements from $B^\pm \rightarrow DK^\pm$

- Reconstruct D in final states accessible to both D^0 and \bar{D}^0
 - $D = D_{\text{CP}}$, CP eigenstates as $K^+ K^-$, $\pi^+ \pi^-$, $K_S \pi^0$
GLW method (Gronau-London-Wyler)
 - $D = D_{\text{sup}}$, Doubly-Cabbibo suppressed decays as $K \pi$
ADS method (Atwood-Dunietz-Soni)
 - Three-body decays as $D \rightarrow K_S \pi^+ \pi^-$, $K_S K^+ K^-$
GGSZ (Dalitz) method (Giri-Grossman-Soffer-Zupan)
- Largest effects due to
 - charm mixing
 - charm CP violation

} negligible
[PRD 72, 031501 (2005)]
- Different B decays (DK , $D^* K$, DK^*)
 - different hadronic factors (r_B , δ_B) for each

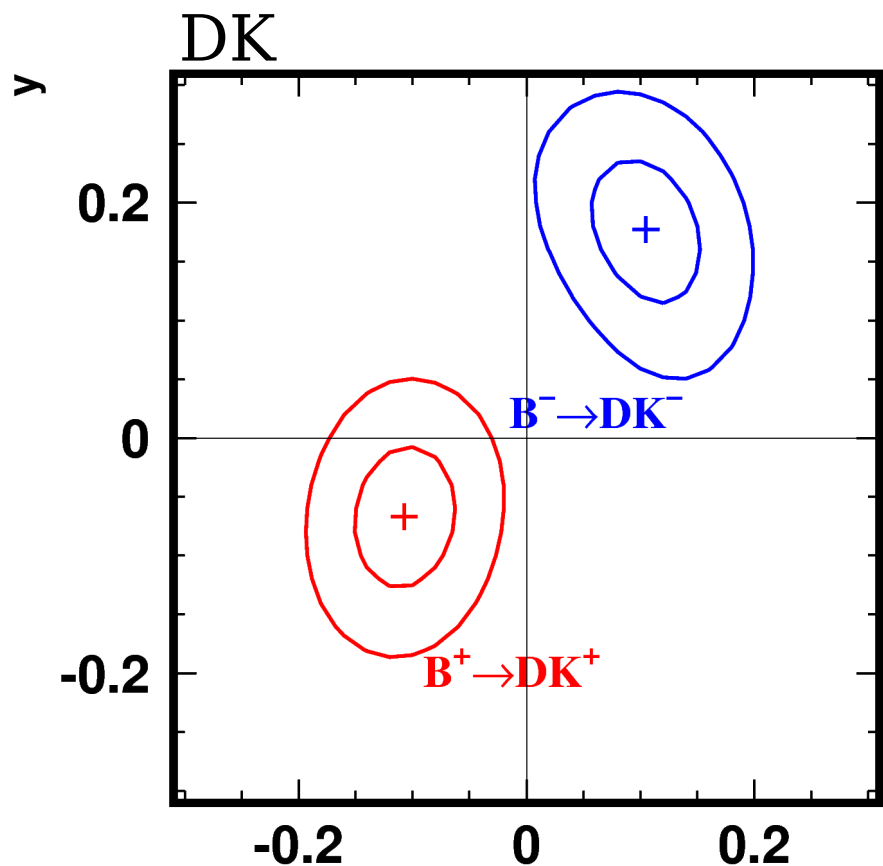
Dalitz $B \rightarrow D^{(*)}(\mathbf{K}_S \pi \pi) \mathbf{K}$

using 605 fb^{-1}

[arXiv:0803.3375]

$$x_{\pm} = r_B \cos(\delta_B \pm \phi_3)$$

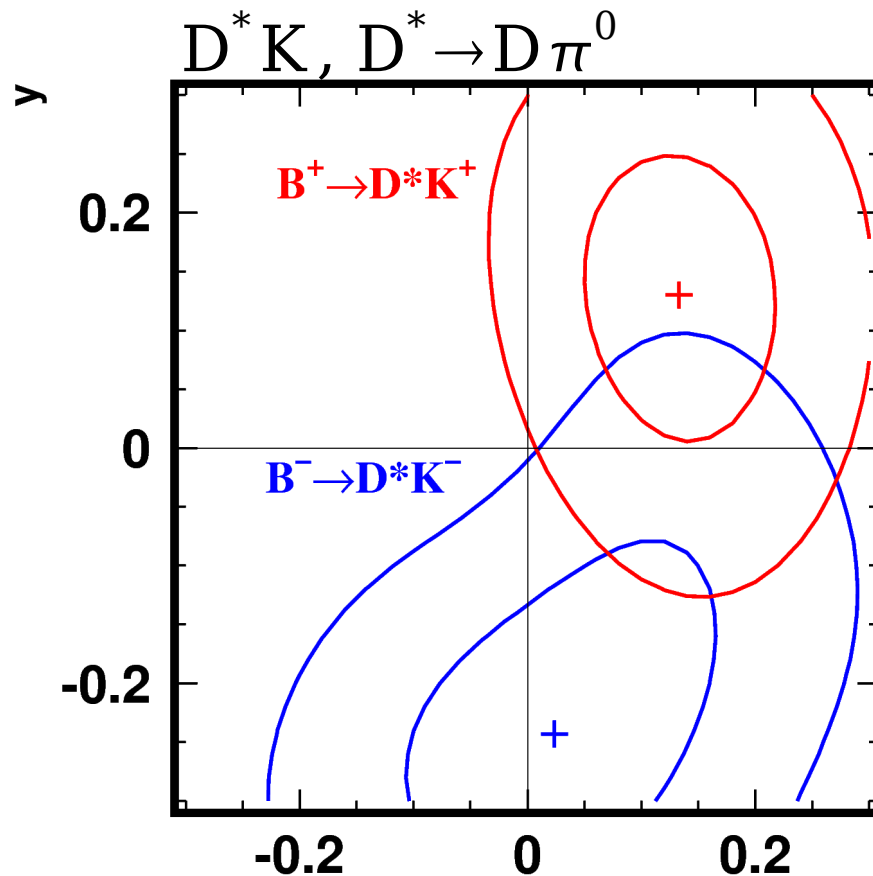
$$y_{\pm} = r_B \sin(\delta_B \pm \phi_3)$$



$$\phi_3 = 80.8^{+13.1}_{-14.8} \pm 5.0 \pm 8.7^\circ \quad \mathbf{x}$$

$$r_B = 0.161^{+0.040}_{-0.038} \pm 0.011 \pm 0.049$$

$$\delta_B = 137.4^{+13.0}_{-15.7} \pm 4.0 \pm 22.9^\circ$$



$$\phi_3 = 63.8^{+20.8}_{-22.9} \pm 4.7 \pm 8.7^\circ \quad \mathbf{x}$$

$$r_B = 0.208^{+0.085}_{-0.083} \pm 0.015 \pm 0.049$$

$$\delta_B = 342.0^{+21.4}_{-22.9} \pm 3.7 \pm 22.9^\circ$$

$$\phi_3 = 76^{+12}_{-13} (\text{stat}) \pm 4 (\text{syst}) \pm 9 (\text{model})$$

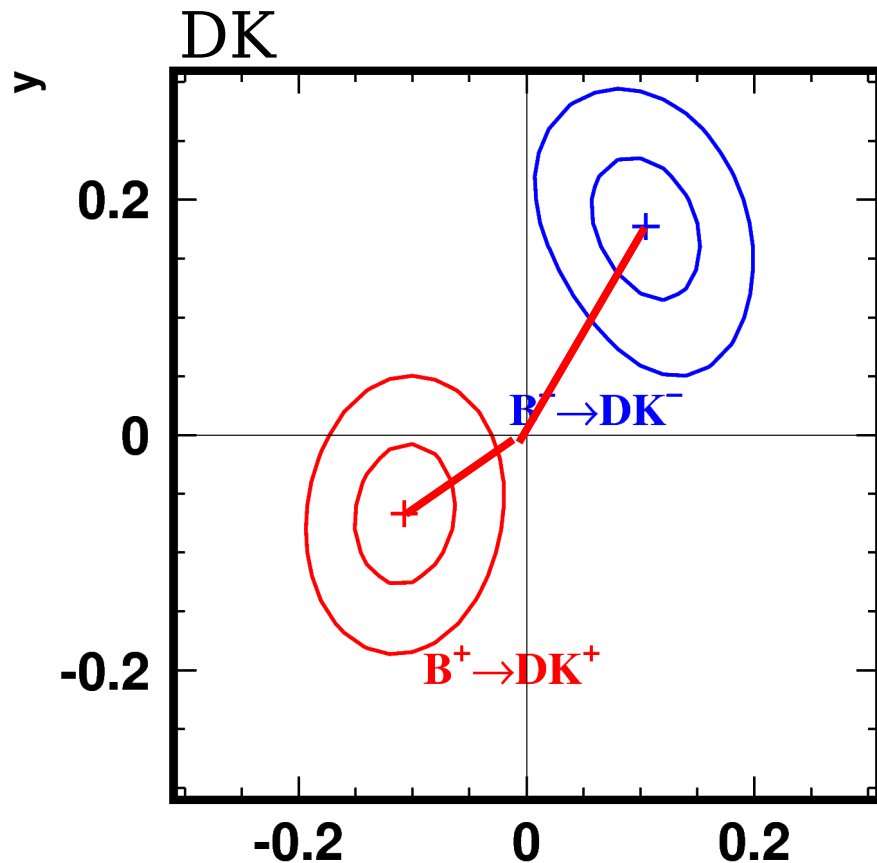
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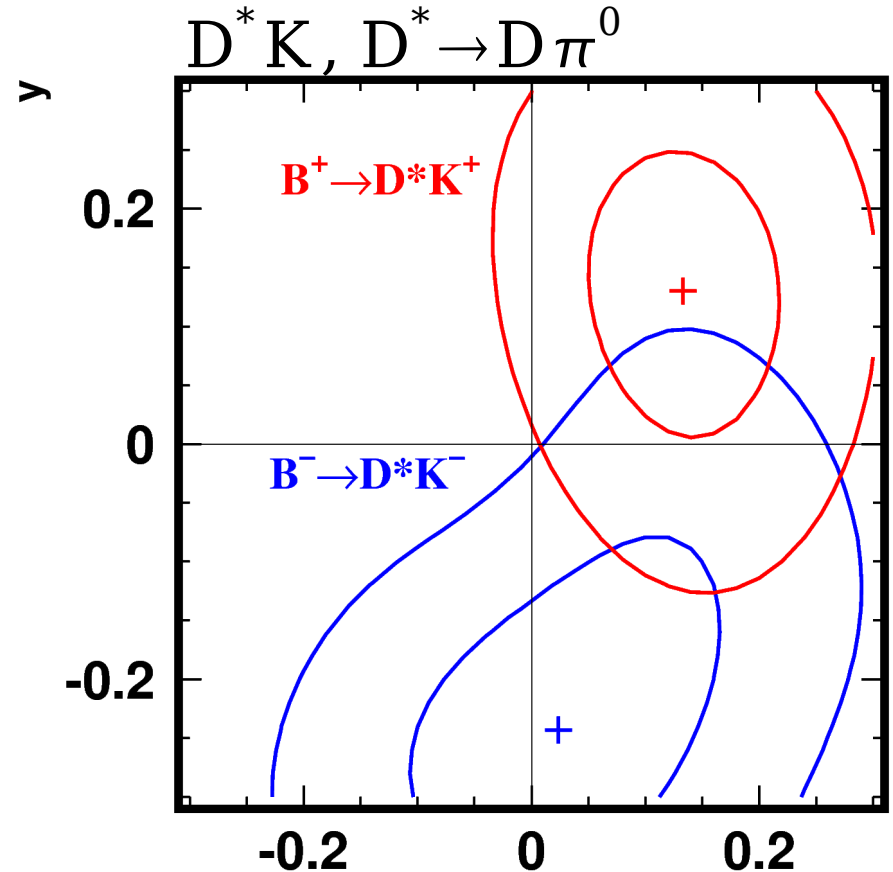
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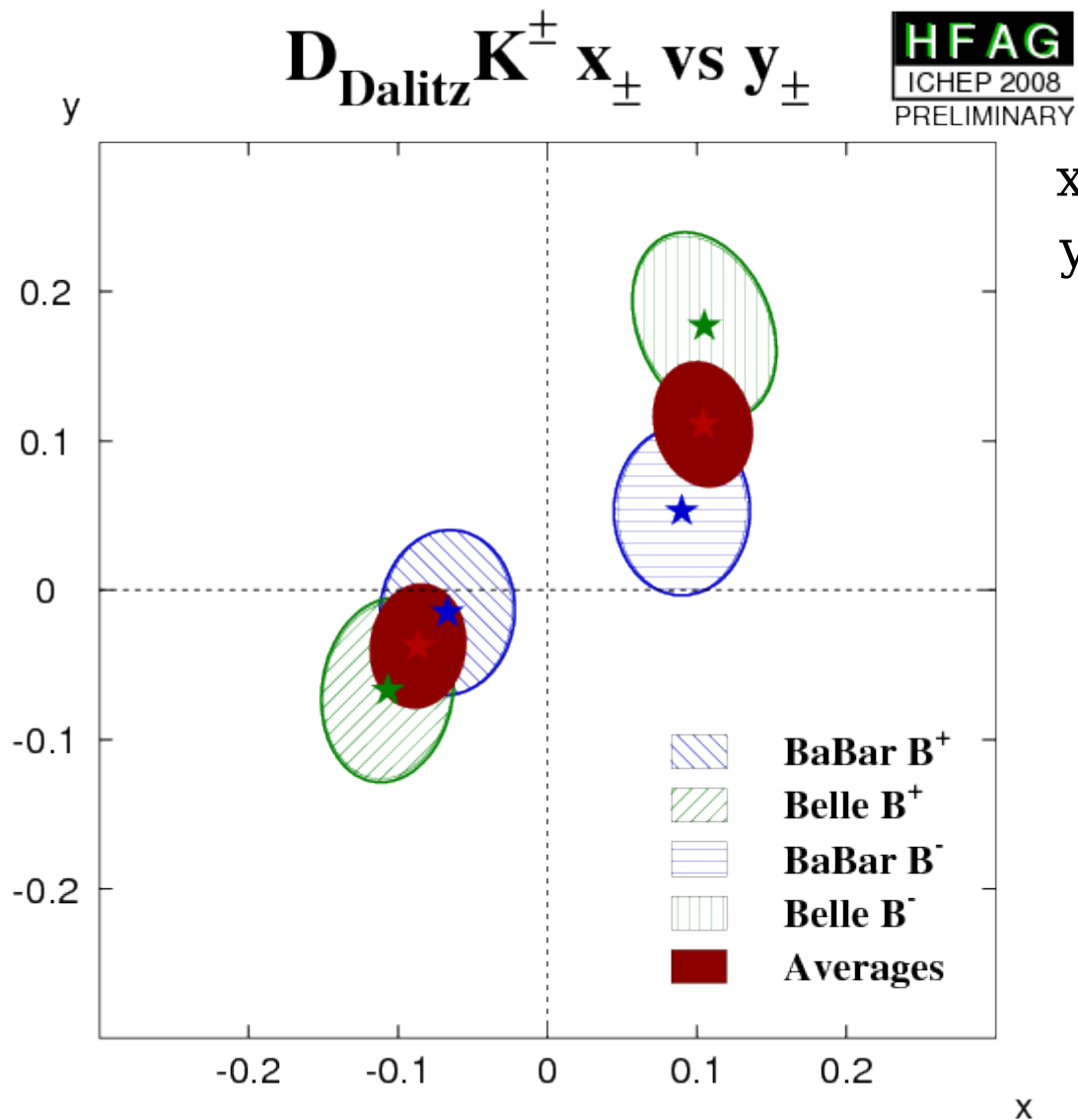
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Dalitz $B \rightarrow DK$



DK, Belle

$$\phi_3 = 80.8^{\circ+13.1}_{-14.8} \pm 5.0 \pm 8.7^{\circ}$$

$$r_B = 0.161^{+0.040}_{-0.038} \pm 0.011 \pm 0.049$$

$$\delta_B = 137.4^{\circ+13.0}_{-15.7} \pm 4.0 \pm 22.9^{\circ}$$

DK, BaBar

$$\phi_3 \sim 63^{\circ} \pm 28^{\circ}$$

$$r_B = 0.086 \pm 0.035$$

$$\delta_B = 109^{\circ+28}_{-31}$$

γ and r_B ... (BaBar example)

analysis with $227 \times 10^6 B\bar{B}$ [**PRL95, 121802 (2005)**]

$$r_B(\text{DK}) = 0.12 \pm 0.08 \pm 0.03 \pm 0.04$$

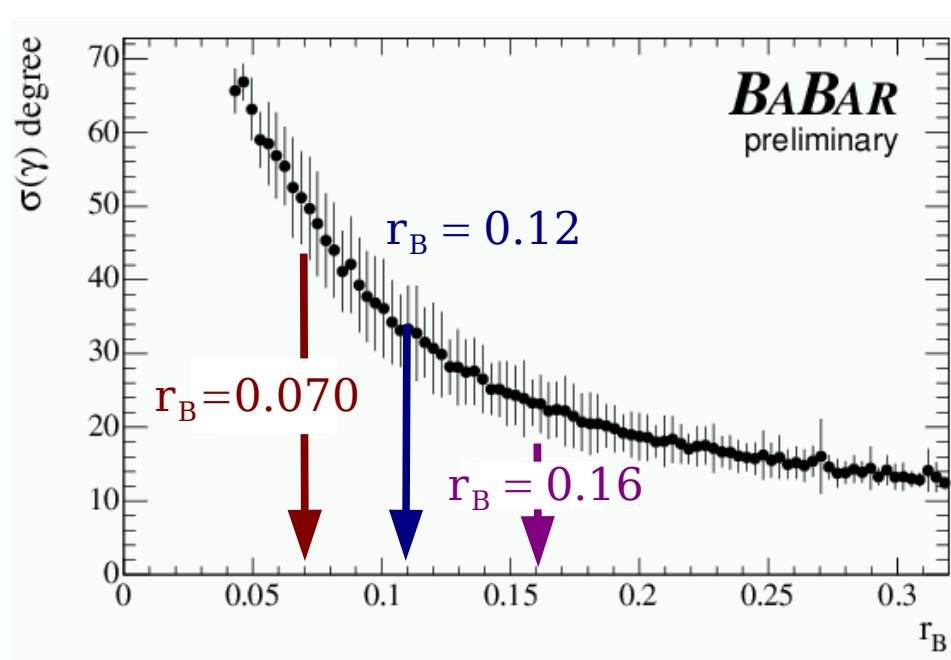
$$\gamma = \mathbf{70^\circ \pm 31^\circ} (\text{stat})_{-10^\circ}^{+12^\circ} (\text{syst})_{-11^\circ}^{+14^\circ} (\text{model})$$

analysis with $347 \times 10^6 B\bar{B}$ [**hep-ex/0607104**] $r_B(\text{DK}) < 0.140$

$$\gamma = \mathbf{92^\circ \pm 41^\circ} (\text{stat}) \pm \mathbf{11^\circ} (\text{syst}) \pm \mathbf{12^\circ} (\text{model})$$

uncertainty on γ scales as $1/r_B$! ($r_B = 0 \Rightarrow$ no constraint on γ)

DK case



- the r_B assumption for the extrapolation is very relevant
- as the stat increases, the sophisticate statistical treatment not necessary anymore

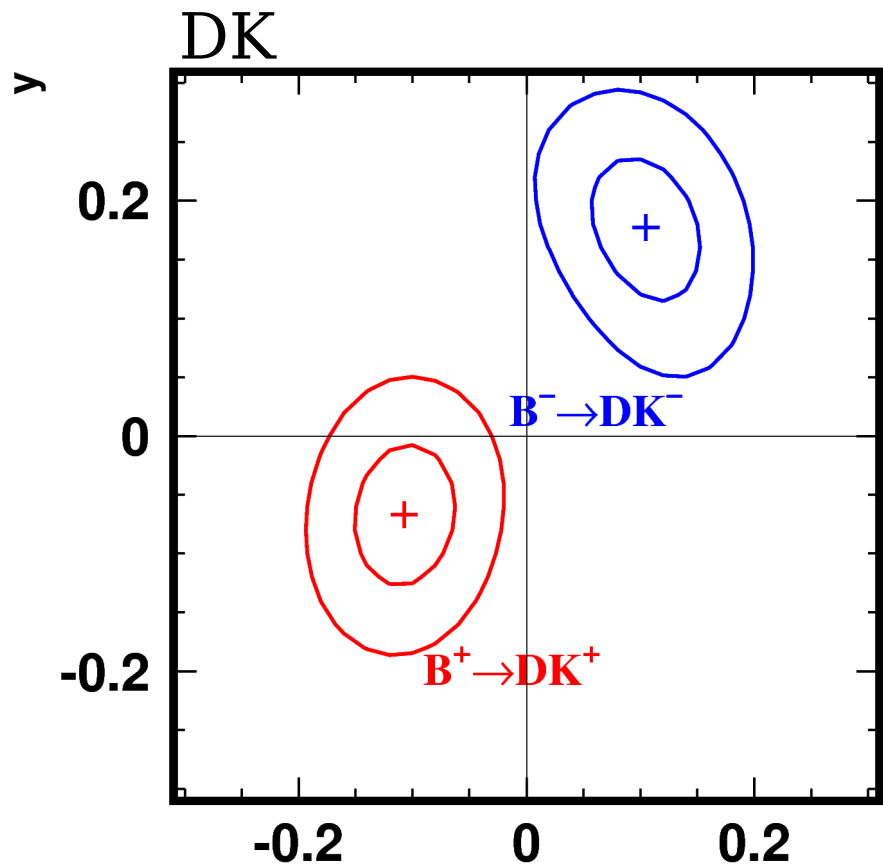
Dalitz $B \rightarrow D^{(*)}(\mathbf{K}_S \pi \pi) \mathbf{K}$

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[arXiv:0803.3375]

$$x_{\pm} = r_B \cos(\delta_B \pm \phi_3)$$

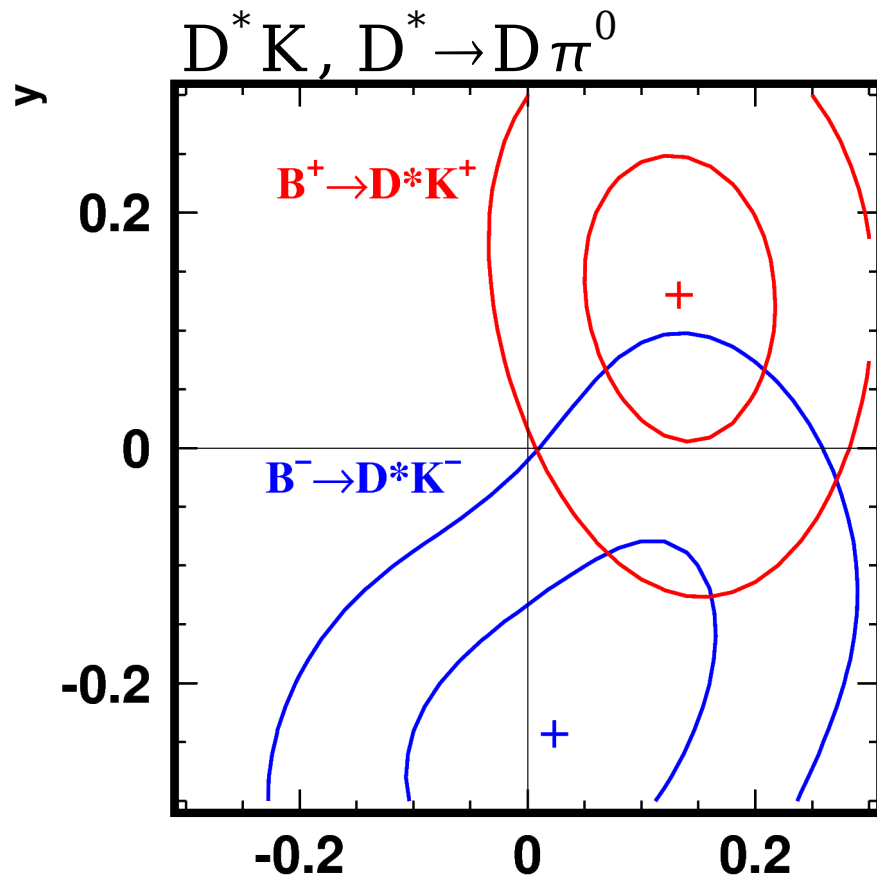
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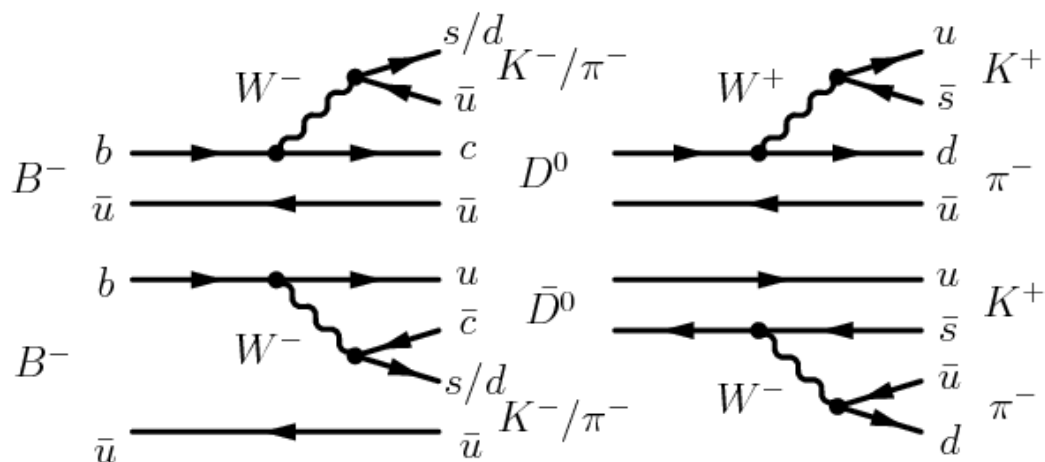
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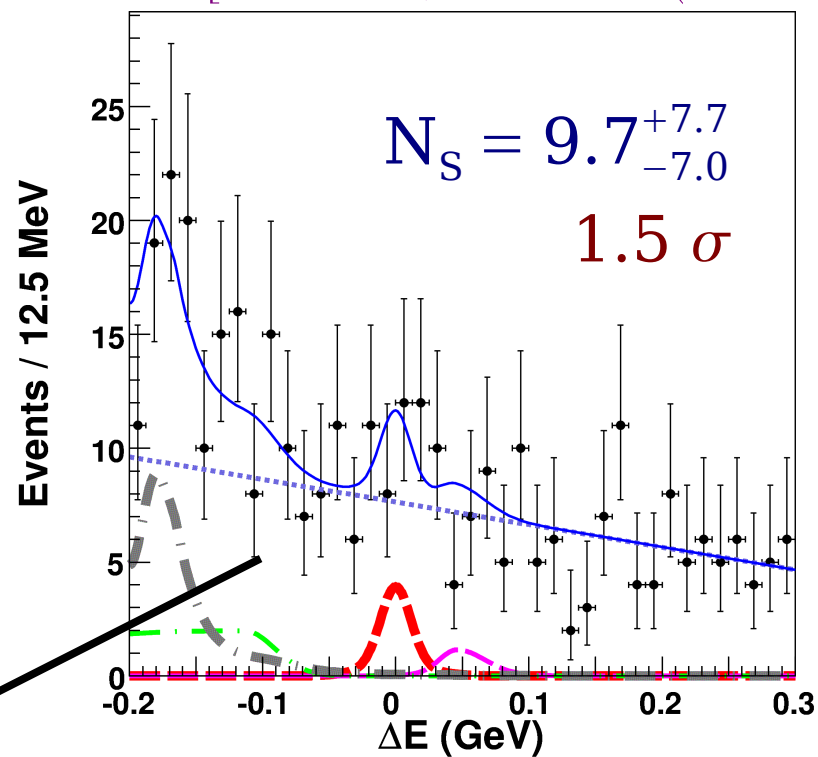
$$\phi_3 = 76^{+12}_{-13} (\text{stat}) \pm 4 (\text{syst}) \pm 9 (\text{model})$$

ADS method: $D \rightarrow K\pi$



- interfering amplitudes are comparable
- introduce 2 new parameters: r_D, δ_D
- but measured by CLEO (\rightarrow BESIII)
- continuum background dominates

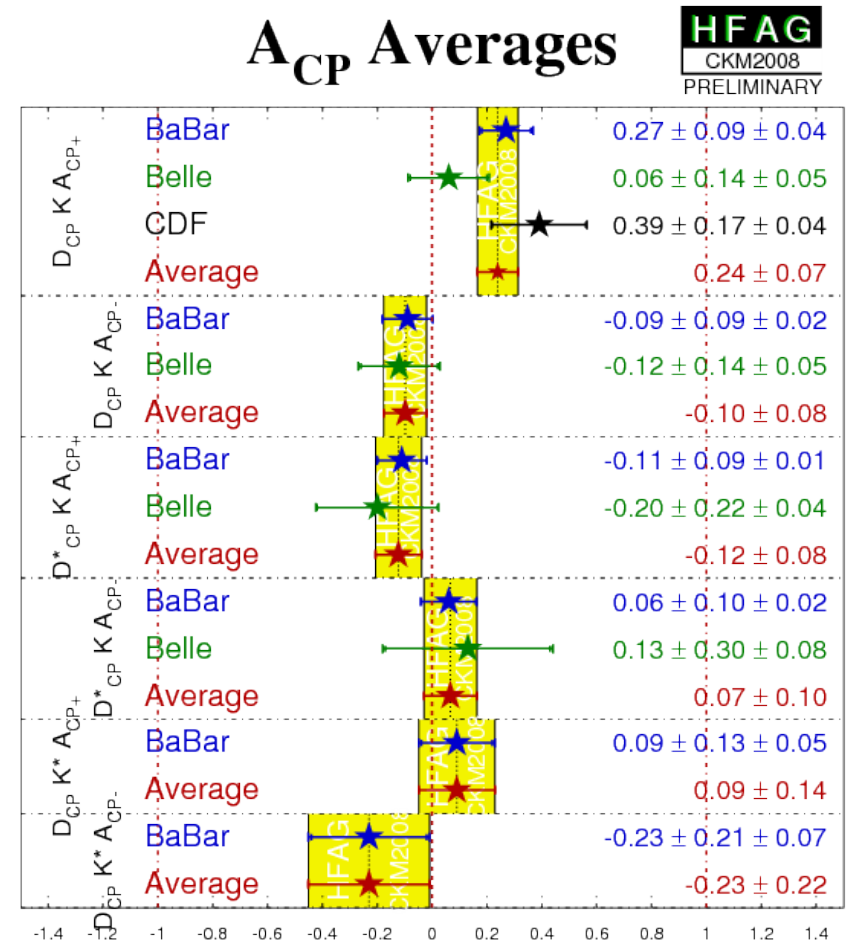
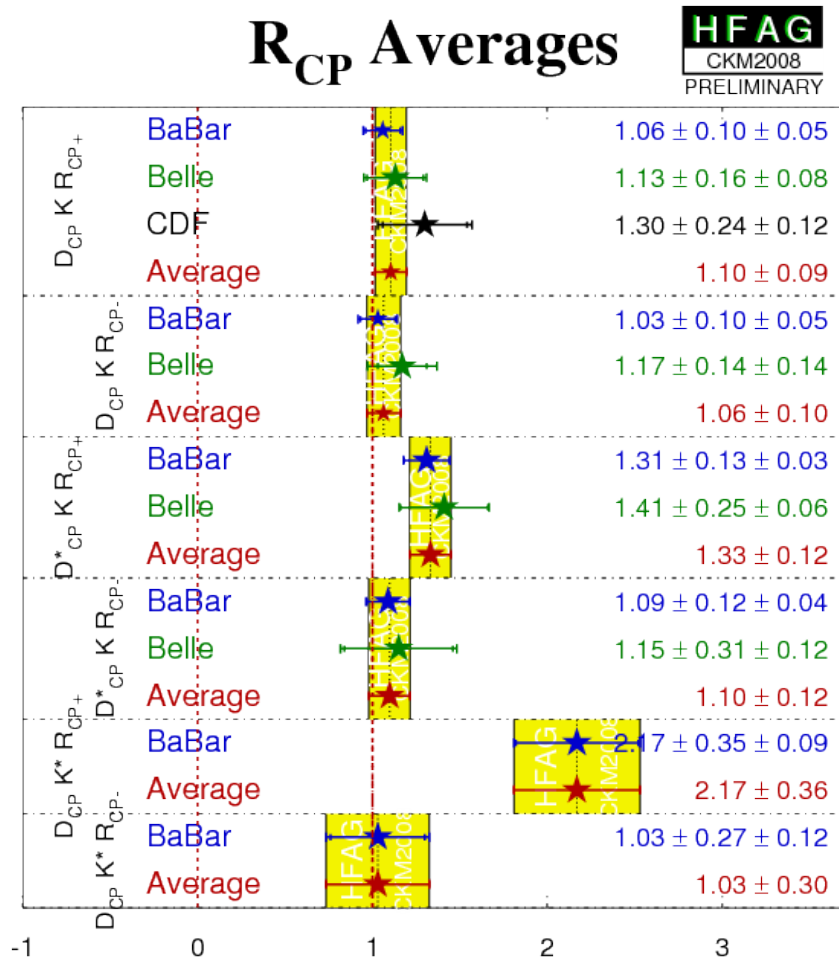
[PRD 78, 071901 (2008)]



continuum

GLW method

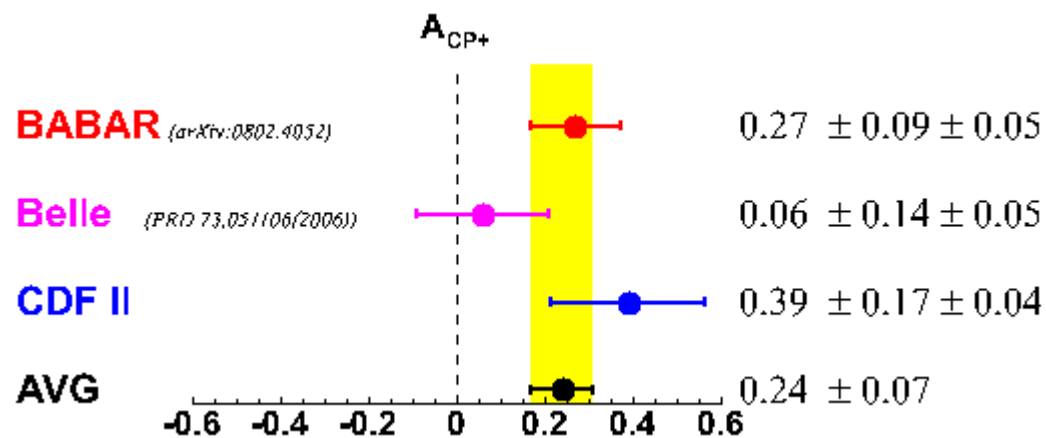
observables R_{CP^\pm} , A_{CP^\pm}



- no charge asymmetry yet observed
- BaBar ($\sim 350 \text{ fb}^{-1}$), Belle ($\sim 250 \text{ fb}^{-1}$)

Other than B-factories: CDF result, ICHEP08

even with a very modest PID system...

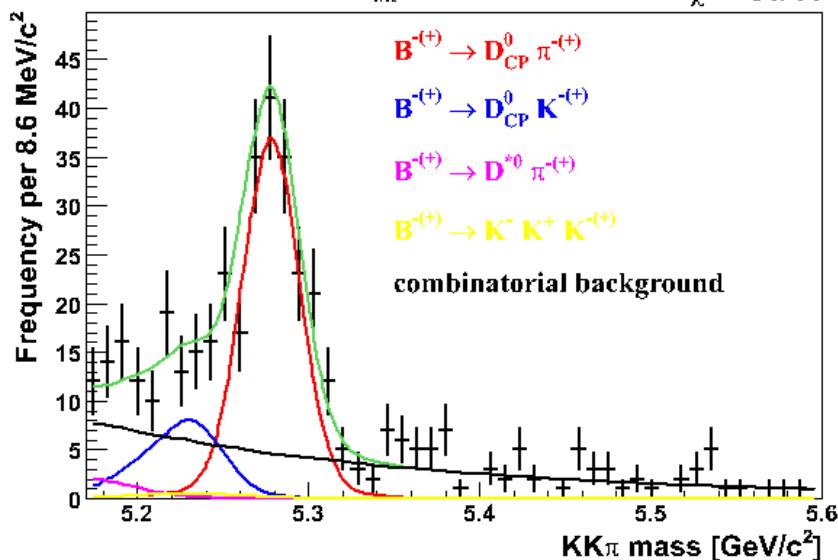


mass projection on a kaon enriched sample ($k > 0.5$)

$D_{CP}(\rightarrow K^+ K^-)K$

CDF Run II Preliminary $L_{int} = 1 \text{ fb}^{-1}$

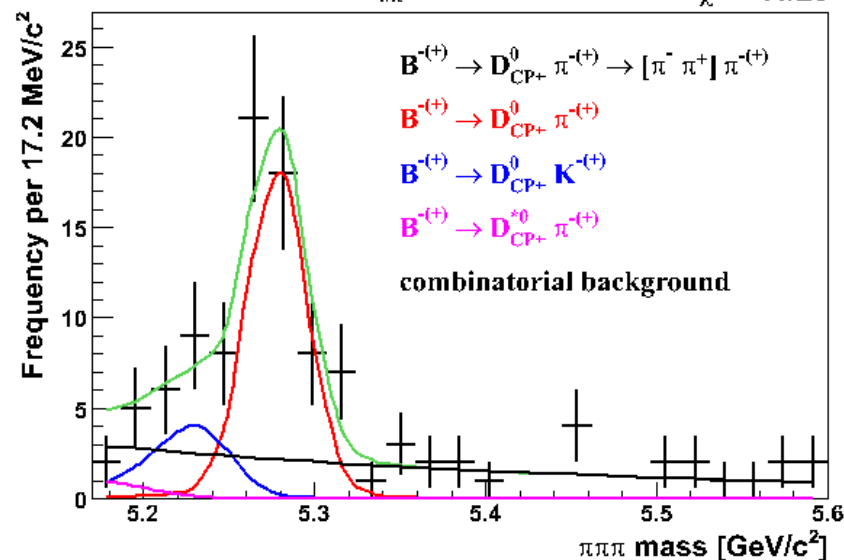
$\chi^2 = 31/44$



$D_{CP}(\rightarrow \pi^+ \pi^-)K$

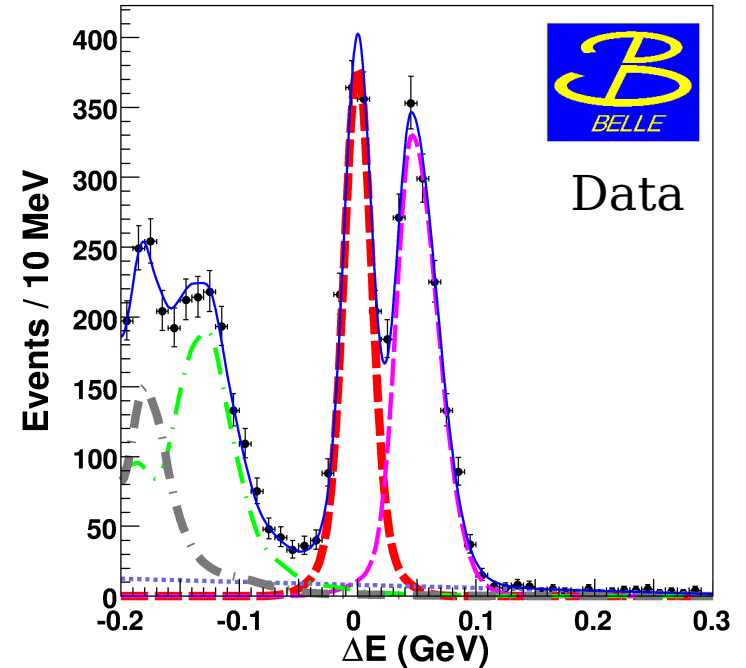
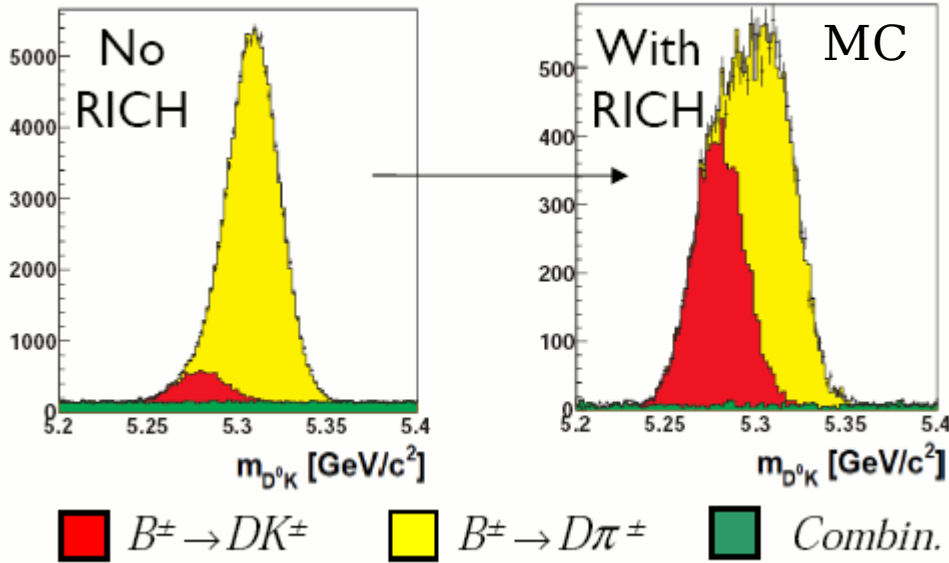
CDF Run II Preliminary $L_{int} = 1 \text{ fb}^{-1}$

$\chi^2 = 11/20$



Predictions for LHCb

PID system (RICH) crucial for LHCb



	LHCb	Belle
Luminosity (fb^{-1})	2	605
$B \rightarrow D_{\text{fav}} K$ yields	28,000	1,220

- good benchmark for the sBelle PID system
- often two kaons in final state: GLW $D(KK)K$, ADS $D(K\pi)K$

Predictions for LHCb

GLW (KK, $\pi\pi$), ADS(K π) for DK⁺

- $K_S\pi^0$ not considered !

- typical statistics for 2 fb⁻¹

Mode	Yield
B → D _{sup} K	650
B → D(KK)K	3,000
B → D($\pi\pi$)K	1,000

good estimation for ADS ?

10 vs 1,220

650 vs 28,000

**Belle ADS: $q\bar{q}$ background dominates
need to improve continuum rejection**

- $\sigma_{\phi_3} \sim (11-14)^\circ$ with $r_B = 0.1$

reasonable assumption

- add ADS mode D(K3 π)K → $\sigma_{\phi_3}(B^+) \sim (7-9.5)^\circ$
determination of $r_D(K3\pi)$ possible at CLEOc

B⁰ → D(hh)K^{*0} sensitivity (2 fb⁻¹)

- assumed $r_{B^0} = 0.4$

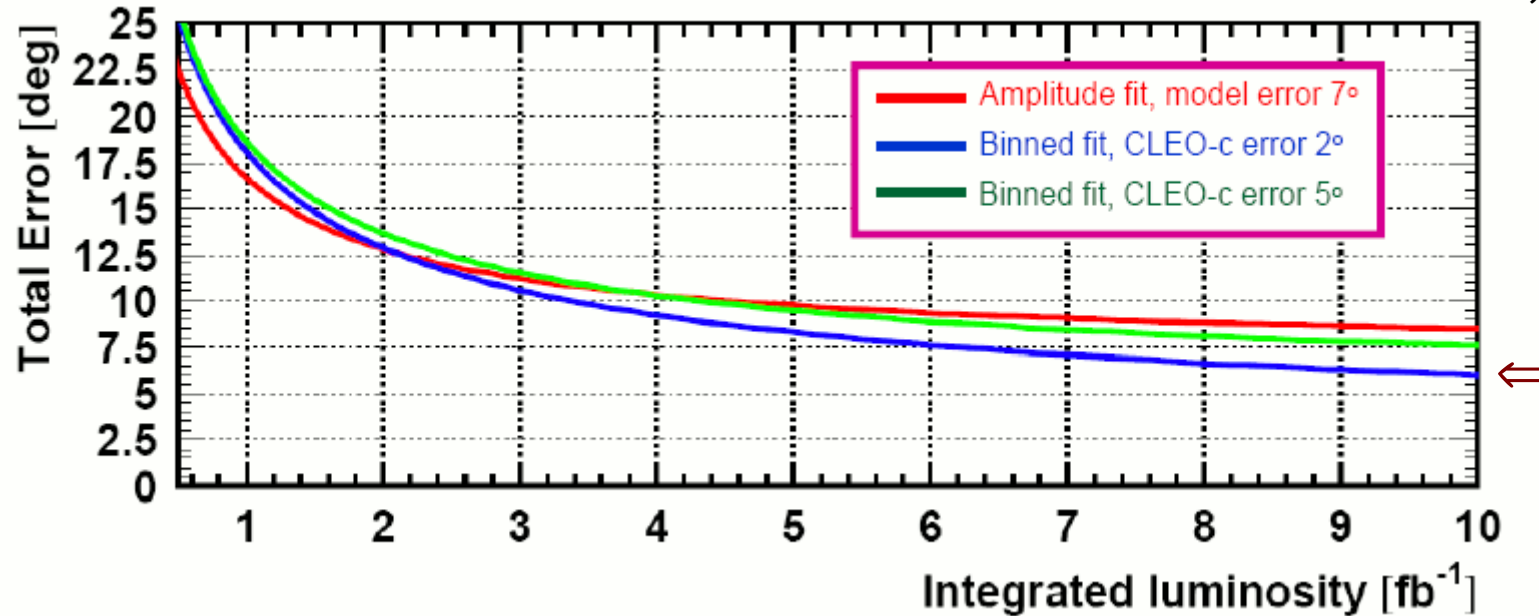
probably too optimistic

- $\sigma_{\phi_3}(B^0) \sim (5.0-13.0)^\circ$

Predictions for LHCb

Dalitz, $D(K_S \pi \pi)K$

G.Wilkinson, CKM08



→ 10 fb^{-1} error on ϕ_3 of 6°

including all measurements

3 categories above and time-dep measurements ($B^0 \rightarrow D\pi$, $B_s \rightarrow D_s K$)

δ_{B^0} ($^\circ$)	0	45	90	135	180
σ_γ for 0.5 fb^{-1} ($^\circ$)	8.1	10.1	9.3	9.5	7.8
σ_γ for 2 fb^{-1} ($^\circ$)	4.1	5.1	4.8	5.1	3.9
σ_γ for 10 fb^{-1} ($^\circ$)	2.0	2.7	2.4	2.6	1.9

↘
 $\sigma(\phi_3) \sim 10^\circ / 2 \text{ fb}^{-1}$

→ sensitivity to ϕ_3 of LHCb with 10 fb^{-1} : $2-3^\circ$

Predictions for sBelle

Dalitz, $D(K_S \pi \pi)K$

- unbinned fit: model error: 5° (BaBar), 9° (Belle)
- binned fit (model dependent):
 - with BESIII stat ($\sim 15\text{fb}^{-1}$ @ $\psi(3770)$): $\sigma_{x,y} \sim 0.0025$
- experimental syst error (irreducible part): $\sigma_{x,y} \sim 0.003$

F.Martinez-Vidal, CKM08

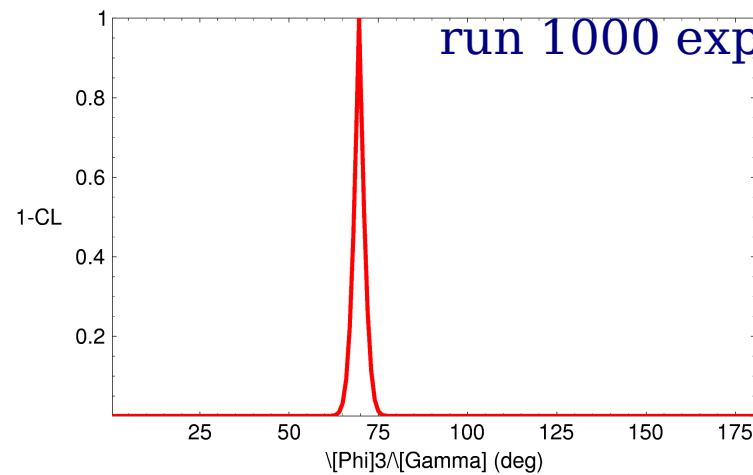
- stat error:

$$- \sigma_{x,y}(\text{DK}) \sim 0.05 \sqrt{\frac{0.6}{50}} \sim 0.005$$

$$- \sigma_{x,y}(\text{D}^* \text{K}) \sim 0.12 \sqrt{\frac{0.6}{50}} \sim 0.013$$

$$- \sigma_{x,y}(\text{DK}^*) \sim 0.20 \sqrt{\frac{0.3}{50}} \sim 0.016$$

assumed $r_B = 0.1$



→ 50 fb⁻¹ error on ϕ_3 of 2° using Dalitz modes

GLW+ADS, DK, D^{*}K, DK^{*}

- no model error
- experimental syst error (irreducible part): $\sigma_{A,R} \sim 0.01$
dominated by detector charge asym
- stat error: just scaled

→ 50 fb⁻¹ error combining with Dalitz ϕ_3 of 1.5°

Conclusion

- still statistically limited, more modes to be included
- work on the assumptions and limiting factors:
sBelle competitive with LHCb, better than 1° will request more than stat

Backup slides